

**CAMBRIDGE INTERNATIONAL EXAMINATIONS**

Cambridge International Advanced Subsidiary and Advanced Level

## **MARK SCHEME for the October/November 2015 series**

### **9709 MATHEMATICS**

**9709/42**

Paper 4, maximum raw mark 50

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes should be read in conjunction with the question paper and the Principal Examiner Report for Teachers.

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## Mark Scheme Notes

Marks are of the following three types:

**M** Method mark, awarded for a valid method applied to the problem. Method marks are not lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, e.g. by substituting the relevant quantities into the formula. Correct application of a formula without the formula being quoted obviously earns the M mark and in some cases an M mark can be implied from a correct answer.

**A** Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated method mark is earned (or implied).

**B** Mark for a correct result or statement independent of method marks.

- When a part of a question has two or more “method” steps, the M marks are generally independent unless the scheme specifically says otherwise; and similarly when there are several B marks allocated. The notation DM or DB (or dep\*) is used to indicate that a particular M or B mark is dependent on an earlier M or B (asterisked) mark in the scheme. When two or more steps are run together by the candidate, the earlier marks are implied and full credit is given.
- The symbol  $\nabla$  implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, A or B marks are given for correct work only. A and B marks are not given for fortuitously “correct” answers or results obtained from incorrect working.
- Note: B2 or A2 means that the candidate can earn 2 or 0.  
B2/1/0 means that the candidate can earn anything from 0 to 2.

The marks indicated in the scheme may not be subdivided. If there is genuine doubt whether a candidate has earned a mark, allow the candidate the benefit of the doubt. Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored.

- Wrong or missing units in an answer should not lead to the loss of a mark unless the scheme specifically indicates otherwise.
- For a numerical answer, allow the A or B mark if a value is obtained which is correct to 3 s.f., or which would be correct to 3 s.f. if rounded (1 d.p. in the case of an angle). As stated above, an A or B mark is not given if a correct numerical answer arises fortuitously from incorrect working. For Mechanics questions, allow A or B marks for correct answers which arise from taking  $g$  equal to 9.8 or 9.81 instead of 10.

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The following abbreviations may be used in a mark scheme or used on the scripts:

|     |   |
|-----|---|
| AEF | Any Equivalent Form (of answer is equally acceptable)   |
| AG  | Answer Given on the question paper (so extra checking is needed to ensure that the detailed working leading to the result is valid)   |
| BOD | Benefit of Doubt (allowed when the validity of a solution may not be absolutely clear)  |
| CAO | Correct Answer Only (emphasising that no “follow through” from a previous error is allowed)   |
| CWO | Correct Working Only – often written by a ‘fortuitous’ answer   |
| ISW | Ignore Subsequent Working   |
| MR  | Misread   |
| PA  | Premature Approximation (resulting in basically correct work that is insufficiently accurate)   |
| SOS | See Other Solution (the candidate makes a better attempt at the same question)  |
| SR  | Special Ruling (detailing the mark to be given for a specific wrong solution, or a case where some standard marking practice is to be varied in the light of a particular circumstance) |

### **Penalties**

|       |   |
|-------|---|
| MR –1 | A penalty of MR –1 is deducted from A or B marks when the data of a question or part question are genuinely misread and the object and difficulty of the question remain unaltered. In this case all A and B marks then become “follow through” marks. MR is not applied when the candidate misreads his own figures – this is regarded as an error in accuracy. An MR –2 penalty may be applied in particular cases if agreed at the coordination meeting. |
| PA –1 | This is deducted from A or B marks in the case of premature approximation. The PA –1 penalty is usually discussed at the meeting.   |

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|-----------------------------|-------------|---|--|---|---|
| <b>1</b>                    | <b>(i)</b>  | $15 + F\cos 60^\circ = F\cos 30^\circ$<br>$F = 41.0$  | <b>M1</b><br><b>A1</b><br><b>A1</b>    | 3 | <b>AG</b> $F = 15(1 + \sqrt{3})$<br>For resolving forces in the $x$ direction   |
|                             | <b>(ii)</b> | $[G = F(\sin 30^\circ + \sin 60^\circ)]$<br>$G = 56.0$  | <b>M1</b><br><b>A1</b>                 | 2 | For resolving forces in the $y$ direction<br>Allow $15(2 + \sqrt{3})$   |
| <b>2</b>                    | <b>(i)</b>  | $[V^2 = (V - 10)^2 + 2g \times 35]$<br>$20V = 100 + 70g$<br>$V = 40$  | <b>M1</b><br><b>A1</b><br><b>A1</b>    | 3 | For using $v^2 = u^2 + 2gs$ to obtain an equation in $V$ only <b>or</b> to obtain two equations in $V$ and $H$ and attempting to eliminate $H$      |
| <b>Alternative for 2(i)</b> |             |   |  |   |   |
|                             | <b>(i)</b>  | $V = V - 10 + 10t \rightarrow t = 1$ and<br>$35 = (V - 10) \times 1 + \frac{1}{2} \times 10 \times 1^2$ or<br>$35 = (V - 10 + V)/2 \times 1$<br>$V = 40$    | <b>M1</b><br><b>A1</b><br><b>A1</b>    | 3 | A complete method to find $V$ by considering the final 35 m using $v = u + at$ and either<br>$s = ut + \frac{1}{2}at^2$ or $s = (u + v)/2 \times t$ |
|                             | <b>(ii)</b> | $[40^2 = 0^2 + 20H]$<br>$H = 80$  | <b>M1</b><br><b>A1</b>                 | 2 | For using $v^2 = u^2 + 2gs$   |
| <b>3</b>                    | <b>(i)</b>  | $[a(t) = 0.00012t^2 - 0.012t + 0.288]$<br>$[a(t) = 0.00012(t^2 - 100t + 2400)$<br>$= 0.00012(t - 40)(t - 60) = 0]$<br>$a(t) = 0$ when $t = 40$ and $t = 60$ | <b>M1*</b><br><b>dM1*</b><br><b>A1</b> | 3 | For attempting to differentiate $v(t)$<br>For setting $a(t) = 0$ and attempting to solve a three term quadratic                                     |
|                             | <b>(ii)</b> | $[0.00001t^4 - 0.002t^3 + 0.144t^2]$<br>$[0.00001(100)^4 - 0.002(100)^3 + 0.144(100)^2]$<br>Displacement is 440 m   | <b>M1†</b><br><b>dM1†</b><br><b>A1</b> | 3 | For attempting to integrate $v(t)$<br>Integration attempted using correct limits $t = 0$ to $t = 100$   |

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| <b>4</b>  | Frictional force = $0.4 \times 2 \cos 45$<br>= $0.4\sqrt{2}$   | <b>M1</b> | 6 | For using $R = 2\cos 45^\circ$<br>and $F = \mu R$<br><br>For using KE gain from $A$ to $C$<br>= PE loss from $A$ to $C$ – Work done by frictional force |
|   | KE gain = $\frac{1}{2} \times 0.2 \times V_C^2$ and<br>PE loss = $0.2 \times g \times (2.5 + 2\sqrt{2})$ | <b>A1</b> |   |   |
|   |  | <b>B1</b> |   |   |
|   | $0.1 V_C^2 = (5 + 4\sqrt{2}) - 0.4\sqrt{2} \times 4$   | <b>M1</b> |   |   |
|   | Speed at $C$ is $9.16 \text{ ms}^{-1}$   | <b>A1</b> |   |   |
| <b>First alternative for the last four marks</b>  |  |           |   |   |
|   | $\frac{1}{2} \times 0.2 \times V_B^2 = 0.2 \times g \times 2.5 \rightarrow$<br>$V_B^2 = 50$              | <b>B1</b> |   | For using KE gain from $B$ to $C$ = PE loss from $B$ to $C$ – Work done by frictional force   |
|   | $0.1 (V_C^2 - V_B^2)$<br>= $0.2 \times g \times (4 \div \sqrt{2}) -$<br>$0.4\sqrt{2} \times 4$           | <b>M1</b> |   |   |
|   |  | <b>A1</b> |   |   |
|   | Speed at $C$ is $9.16 \text{ ms}^{-1}$   | <b>A1</b> |   |   |
| <b>Second alternative for the last four marks</b> |  |           |   |   |
|   | $\frac{1}{2} \times 0.2 \times V_B^2 = 0.2 \times g \times 2.5 \rightarrow$<br>$V_B^2 = 50$              | <b>B1</b> |   | For using Newton's 2 <sup>nd</sup> law to find acceleration along $BC$ <b>and</b> using $v^2 = u^2 + 2as$ to find $V_C$                                 |
|   | $\sqrt{2} - 0.4\sqrt{2} = 0.2a \rightarrow a$<br>= $3\sqrt{2} \text{ ms}^{-2}$                           | <b>M1</b> |   |   |
|   | and $V_C^2 = V_B^2 + 2 \times 3\sqrt{2} \times 4$  | <b>A1</b> |   |   |
|   | Speed at $C$ is $9.16 \text{ ms}^{-1}$   | <b>A1</b> |   |   |

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| <p>5 (i)</p> $0.5g \times \frac{7}{25} - T = 0.5a$ $T - 0.1g = 0.1a$ $1.4 - 1 = 0.6a$ <p>For eliminating <math>T</math> and obtaining</p> $a = \frac{2}{3} \text{ ms}^{-2}$ <p>Tension is 1.07N</p>  | <p>M1</p> <p>A1</p> <p>B1</p> <p>M1</p> <p>A1</p>           | <p>5</p> | <p>For applying Newton 2<sup>nd</sup> law to <math>P</math> or to <math>Q</math> or for applying N2 to the system</p> <p>Any two correct<br/>Allow sin 16.3 for 7/25</p> <p>For substituting for <math>a</math> to find <math>T</math></p> <p>Allow <math>T = 16/15</math> N</p>   |
| <p>(ii)</p> $[v^2 = 2 \times \left(\frac{2}{3}\right) \times 0.7]$ $[2^2 = 2 \times \frac{2}{3} \times 0.7 + 2 \times 0.28g \times s]$ <p>Length of string = <math>2.5 - s = 1.95</math> m</p>   | <p>M1</p> <p>M1</p> <p>A1</p>                               | <p>3</p> | <p>For using <math>v^2 = u^2 + 2as</math> to find the speed of the particles immediately before the string breaks</p> <p>For applying <math>v^2 = u^2 + 2as</math> for the motion of <math>P</math> when the string is slack and <math>s</math> is the distance travelled by <math>P</math> after the break until it reaches the floor</p> <p>Allow length = 41/21 m</p> |
| <p>6 (i)</p> $[0.195 \cos \theta = F]$ $F = 0.195 \cos 22.6 = 0.195 \times \frac{12}{13}$ $= 0.18 = \frac{9}{50}$ $[R = 0.24 + 0.195 \sin \theta]$ $R = 0.24 + 0.195 \sin 22.6 =$ $0.24 + 0.195 \times \frac{5}{13} = 0.315$ $= \frac{63}{200}$ <p>Coefficient <math>\mu = 4/7</math> or 0.571</p> | <p>M1</p> <p>A1</p> <p>M1</p> <p>A1</p> <p>M1</p> <p>A1</p> | <p>6</p> | <p>For resolving forces horizontally</p> <p>For resolving forces vertically</p> <p>For using <math>\mu = F/R</math></p>  |

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| (ii)  | $R = 0.24 - 0.195 \sin 22.6$ $= 0.24 - 0.195 \times \frac{5}{13}$ $= 0.165 = \frac{33}{200}$<br>$0.195 \times \frac{12}{13} - \left(\frac{4}{7}\right) \times 0.165$ $= 0.024a$<br>Acceleration is $3.57 \text{ ms}^{-2}$                                    | <b>B1</b><br><br><b>M1</b><br><br><b>A1</b><br><br><b>A1</b>                  | 4 | For using Newton's second law for motion along the rod<br><br><br>Allow acceleration = $25/7$  |
| 7 (i) | [WD = $14000 \times 25$ ]<br><br>Work done is 350 kJ or 350 000 J  | <b>M1</b><br><br><b>A1</b>  | 2 | For using $P = WD \div \Delta t$   |
| (ii)  | $14000/v_A - 235 = 1600 \times 0.5 \rightarrow$ $v_A = 13.53 \text{ ms}^{-1}$<br>$14000/v_B - 235 = 1600 \times 0.25 \rightarrow$ $v_B = 22.05 \text{ ms}^{-1}$<br>[KE gain = $\frac{1}{2} 1600(22.05^2 - 13.53^2)$ ]<br><br>KE gain = 242.5 kJ or 242 500 J | <b>M1</b><br><br><b>A1</b><br><br><b>A1</b><br><br><b>M1</b><br><br><b>A1</b> | 5 | For using DF = $P/v$ and Newton's 2 <sup>nd</sup> law to find the speed of the car at <i>A</i> or at <i>B</i><br><br>$v_A = 2800/207$<br><br>$v_B = 2800/127$<br><br>For using KE gain<br>$= \frac{1}{2} m(v_B^2 - v_A^2)$ |
| (iii) | $350\,000 = 242\,500 + 235 \times AB$<br>Distance <i>AB</i> is 457 m   | <b>M1</b><br><br><b>A1</b> <sup>✓</sup><br><br><b>A1</b>                      | 3 | For using WD by DF<br>$= \text{KE gain} + \text{resistance} \times AB$   |