CAMBRIDGE INTERNATIONAL EXAMINATIONS

International General Certificate of Secondary Education

MARK SCHEME for the May/June 2013 series

0580 MATHEMATICS

0580/41 Paper 4 (Extended), maximum raw mark 130

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes should be read in conjunction with the question paper and the Principal Examiner Report for Teachers.

Cambridge will not enter into discussions about these mark schemes.

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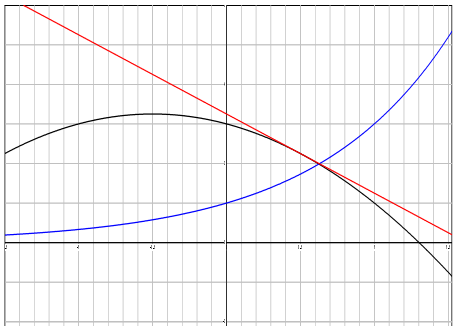
Abbreviations

cao correct answer only
cso correct solution only
dep dependent
ft follow through after error
isw ignore subsequent working
oe or equivalent
SC Special Case
www without wrong working
art anything rounding to
soi seen or implied

Qu.	Answer	Mark	Part marks
1 (a) (i)	[0]8 15	1	
(ii)	$\frac{1.8}{27} \times 60$ [= 4] oe	M2	**M1** for $\frac{1.8}{27}$ oe [0.0667 or better]
(b) (i)	275	3	**M2** for $\frac{15-4}{4} \times 100$ or $\frac{15}{4} \times 100 - 100$ oe or **M1** for $\frac{15-4}{4}$ or $\frac{15}{4} \times 100$ or oe 375
(ii)	73.3[3…]	3	**M2** for $\frac{1.8}{15} \times 60$ [=7.2 min] and $\frac{27 - \textit{their}\ 7.2}{27} \times 100$ oe or **M1** for $\frac{1.8}{15} \times 60$ [=7.2 min] or final answer of 26.6[6…] or 26.7
(iii)	25	2	**M1** for $\frac{9}{\textit{figs}\ 36}$ oe

Qu.	Answer	Mark	Part marks
2 (a)	3, 0.33[3…], 1	3	**B1** for each correct value
(b)	Correct quadratic curve	3	**B2FT** for 7 correct points or **B1FT** for 5 or 6 correct points
	Correct exponential curve 	3	**B2FT** for 7 correct points or **B1FT** for 5 or 6 correct points
(c) (i)	Answer in range $1.2 < x < 1.4$	1	
(ii)	Answer in range $1.2 < x < 1.35$	1	Not from a line other than $y = 4$ (±1mm)
(iii)	Answer in range $0.55 < x < 0.7$	1	
(d)	Correct tangent drawn And answer in range $-2.5 < m < -1.5$	3	**B1** for correct tangent at $x = 0.5$ **B2** for answer in range dep on close attempt at tangent **M1** for $[-]\frac{rise}{run}$ used with values soi from tangent, dep on close attempt at tangent or answer in range $1.5 < m < 2.5$ or **SC1** for close attempt at tangent to exponential curve and answer in the range $1.6 < m < 2.2$
3 (a) (i)	3.2	1	
(ii)	4.2	1	
(iii)	4.6	1	
(iv)	196	1	
(b) (i)	100, 46, 12	2	**B1** for 2 correct
(ii)	4	2	**M1** for frequency of 60 or 140 seen in workspace

Qu.	Answer	Marks	Part marks
4 (a)	Enlargement	1	
	[centre] (–3, 4)	1	Do not allow column vector for coordinates
	[scale factor] 3	1	
(b) (i)	Image at (1 5), (4, 5), (4, 6), (1, 7)	2	**SC1** for translation by $\begin{pmatrix}5\\k\end{pmatrix}$ or $\begin{pmatrix}k\\4\end{pmatrix}$
(ii)	Image at (5, 1), (8, 1), (8, 3), (5, 2)	2	**SC1** for reflection in $y = 2$
(iii)	Image at (– 4, 3), (– 1, 3), (– 1, 6), (– 4, 9)	2	**SC1** for three correct vertices or shape with vertices at (–4, 1) and (–1, 1), (–1, 4) and (–4, 7)
(iv)	$\begin{pmatrix}1 & 0\\0 & 3\end{pmatrix}$	2	**SC1** for $\begin{pmatrix}1 & 0\\0 & k\end{pmatrix}$, k ≠ ± 1 or $\begin{pmatrix}3 & 0\\0 & 1\end{pmatrix}$
(c)	Reflection $y = x$ oe	2	**B1 B1** independent
5 (a)	171.25 (or 171 or 171.2 or 171.3) www	3	**M1** for 5 × 155 + 9 × 162.5 + 18 × 172.5 + 10 × 185 [= 7192.5] and **M1** (dep on **M1**) for *their* Σ*fx* ÷ 42
(b)	$160 < x \leq 165$ oe	1	
(c)	Blocks with heights of 1.8, 1.2, 1, with correct interval widths and no gaps	4	**B3** for 2 correct blocks or **B2** for 1 correct block or **B1** for 3 correct frequency densities or heights or 3 correct widths

Qu.	Answer	Marks	Part marks
6 (a)	31.4	3	**M2** for $\frac{15.7}{\sin 30}$ or **M1** for correct implicit statement
(b)	[sin$E$ =] $\frac{15.7 \times \sin 52}{16.5}$	M2	**M1** for correct implicit statement
	48.573…	A1	
(c) (i)	[$\angle ACE$ =] 180 – 52 – 48.57	M1	
	[= 79.43]		
	[$\angle ECD$ =] 40.57…	A1	
(ii)	15.3 or 15.27 to 15.281 www	4	**M2** for [$(DE)^2$ =] $16.5^2 + 23.4^2 - 2 \times 16.5 \times 23.4\cos(40.6$ or $40.57)$ or **M1** for full correct implicit statement **A1** for 233 to 234
(d)	466 or 466.34 to 466.5	4	**M1** for $0.5 \times 15.7 \times$ *their* 31.4 sin(90 – 30) oe **M1** for $0.5 \times 15.7 \times 16.5$ sin(128 – *their* 48.6 or 48.57) oe **M1** for $0.5 \times 16.5 \times 23.4$ sin (40.6 or 40.57) oe

Qu.	Answer	Mark	Part marks
7 (a)	6.61 (6.614…) www	6	**B1** for $\frac{x+2}{2x+3} = \frac{9}{16}$ oe **M1** for $16(x + 2) = 9(2x + 3)$ or better **A1** for [x =] 2.5 **M2** for $\sqrt{\{(2 \times \textit{their}\ x + 3)^2 - (\textit{their}\ x + 2)^2\}}$ or **M1** for $(2 \times \textit{their}\ x + 3)^2 - (\textit{their}\ x + 2)^2$ or **SC2** for final answer of $4\sqrt{13}$ or $\frac{7\sqrt{15}}{2}$ or better **SC1** for final answer of $5\sqrt{7}$ or better
(b) (i)	White = 8.5, red = 11	5	**B3** for $7w + 5(w + 2.5) = 114.5$ or for $7(r - 2.5) + 5r = 114.5$ oe **B1** for 8.5 or 11 or **SC2** for $7w + 5 \times w + 2.5 = 114.5$ leading to 9.33[3…] or **SC1** for $7w + 5 \times w + 2.5 = 114.5$ OR **B1** for $r = w + 2.5$ oe **B1** for $7w + 5r = 114.5$ oe **M1** for elimination of a variable **A1** for 8.5 or 11
(ii) (a)	$\frac{42}{132}$ or $\frac{21}{66}$ or $\frac{14}{44}$ or $\frac{7}{22}$ (0.318 or 0.3181 to 0.3182)	2	**M1** for $\frac{7}{12} \times \frac{6}{11}$
(ii) (b)	$\frac{70}{132}$ or $\frac{35}{66}$ (0.53[0] or 0.5303…)	3	**M2** for $\frac{7}{12} \times \frac{5}{11} + \frac{5}{12} \times \frac{7}{11}$ or $1 - \textit{their}$ (a) $- \frac{5}{12} \times \frac{4}{11}$ or **M1** for $\frac{7}{12} \times \frac{5}{11}$ or $\frac{35}{132}$ or **SC1** for $\frac{70}{144}$ oe from replacement

Qu.	Answer	Mark	Part marks
8 (a) (i)	118	2	**M1** for $(3 \times 180 - 2 \times 110 - 84)$ [÷ or better
(ii)	31	1FT	FT $(180 - \textit{their}$ (i)$) \div 2$
(iii)	22	1FT	FT $84 - 2 \times$ *their* (ii) or $2 \times$ *their* (ii) $- 40$, only if positive answer and less than 84
(b)	32	4	**B2** for $360 - 3y = 2(4y + 4)$ oe and **B1** for $11y = 352$ oe or **M1** for angle at centre = 2 × angle at circumference soi
(c) (i)	Opposite angles [cyclic quad] add to 180	1	
(ii)	68	3	**M1** for [angle *PRS* =] $102 \div 3 \times 2$ and **M1** for angle *PQS* = angle *PRS* or angle *PRQ* = angle *PSQ*
(d)	5.75	3	**M2** for $6.9 \times \sqrt{\frac{5}{7.2}}$ oe or **M1** for evidence of ratio of areas = (ratio of sides)^2 or sf = 1.2
9 (a)	$\frac{-1 \pm \sqrt{1^2 - 4 \times 1 \times (-3)}}{2}$	2	**B1** for $\sqrt{1^2 - 4 \times 1 \times (-3)}$ or better and if in the form $\frac{p + \sqrt{q}}{r}$ or $\frac{p - \sqrt{q}}{r}$
	–2.30, 1.30 final answer	2	then **B1** for $p = -1$ and $r = 2(1)$ or better **B1 B1** **SC1** for –2.30 and 1.30 seen or –2.3 or –2.303 to – 2.302 **and** 1.3 or 1.302 to 1.303 or final answer –1.30 and 2.30
(b)	4, 30, 53	3	**M1** for $(2x + 7)^2 + (2x + 7) - 3$ and **B1** for $(2x + 7)^2 = 4x^2 + 14x + 14x + 49$ oe

Qu.	Answer	Mark	Part marks
(c)	$\frac{x-7}{2}$	2	**M1** for $y - 7 = 2x$ or $x = 2y + 7$ or -7 **then** ÷ 2 clearly seen in correct order with arrow or better or $\frac{y-7}{2}$
(d)	–2	1	
(e)	1.158×10^{77}	4	**B3** for 1.16×10^{77} or $1.1579\ldots \times 10^{77}$ or 1.157×10^{77} or **B2** for 2^{256} seen or **B1** for 2^8 seen or 256
10 (a)	50, 70	1	
	$10n$ oe	1	
	51, 71	1	
	$10n + 1$ oe	1	
(b) (i)	212	1	
(ii)	$20n + 12$	1	
(iii)	$20n + 152$	1	
(c) (i)	$5 \times 3^2 + 6 \times 3 = 63$	1	
	and $11 + 21 + 31 = 63$		
	or $32 + 31 = 63$ or $11 + 52 = 63$	1	
(ii)	560	1	
(d)	Complete solution with no errors seen and a conclusion e.g. $5n^2 + 6n + 10(n + 1) + 1$ $= 5n^2 + 6n + 10n + 10 + 1$ $= 5n^2 + 10n + 5 + 6n + 6$ $= 5n^2 + 10n + 5 + 6n + 6$ $= 5(n + 1)^2 + 6(n + 1)$	4	**B1** for $5n^2 + 6n + 10n + 10 + 1$ or better **B1** for use of $5(n + 1)^2 = 5n^2 + 10n + 5$ oe at any stage **B1** for use of $6n + 6 = 6(n + 1)$ oe at any stage