## Cambridge IGCSE ${ }^{\text {TM }}$

CANDIDATE
NAME
CENTRE NUMBER

CANDIDATE NUMBER

Paper 5 Investigation (Core)

You must answer on the question paper.
No additional materials are needed.

## INSTRUCTIONS

- Answer all questions.
- Use a black or dark blue pen. You may use an HB pencil for any diagrams or graphs.
- Write your name, centre number and candidate number in the boxes at the top of the page.
- Write your answer to each question in the space provided.
- Do not use an erasable pen or correction fluid.
- Do not write on any bar codes.
- You should use a graphic display calculator where appropriate.
- You may use tracing paper.
- You must show all necessary working clearly, including sketches, to gain full marks for correct methods.
- In this paper you will be awarded marks for providing full reasons, examples and steps in your working to communicate your mathematics clearly and precisely.


## INFORMATION

- The total mark for this paper is 36 .
- The number of marks for each question or part question is shown in brackets [ ].

Answer all the questions.

## INVESTIGATION

AREA OF RIGHT-ANGLED TRIANGLES

This investigation looks at finding the area of a right-angled triangle using its perimeter.
In this investigation all lengths are in centimetres.

$w$ is the hypotenuse of the triangle, $b$ is the base of the triangle, $h$ is the height of the triangle.

Perimeter, $P$, of this triangle.
$P=b+h+w$
Area, $A$, of this triangle.
$A=\frac{1}{2} b h$

1 (a)


This right-angled triangle is drawn on a $1 \mathrm{~cm}^{2}$ grid.
(i) Measure and write down the length of the hypotenuse.
(ii) Show that the perimeter is 12 .
(iii) Find the area of the triangle.
(b)

(i) Find the perimeter of this triangle.
(ii) Find the area of this triangle.
(c)


Complete the table for right-angled triangles with sides $b, h$ and $w$.

| $b$ | $h$ | $w$ | Perimeter, $P$ | Area, $A$ |
| :---: | :---: | :---: | :---: | :---: |
| 12 | 5 | 13 | 30 | 30 |
| 84 | 13 | 85 |  |  |
| 24 |  | 25 | 56 | 84 |
| 60 | 11 |  | 132 |  |

2 (a)


This triangle has perimeter $P=60$.
Show that the calculation $\frac{60}{2} \times\left(\frac{60}{2}-26\right)$ gives the correct area for this triangle.
(b)


This triangle has perimeter $P=112$.
Show that the calculation $\frac{112}{2} \times\left(\frac{112}{2}-50\right)$ gives the correct area for this triangle.

3 (a) Complete the table.

| $b$ | $h$ | $w$ | $P$ | $A$ | Calculation |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :--- |
| 24 | 10 | 26 | 60 | 120 | $\frac{60}{2} \times\left(\frac{60}{2}-26\right)$ | $=120$ |
| 12 | 9 | 15 | 36 | 54 | $\frac{36}{2} \times\left(\frac{36}{2}-15\right)$ | $=$ |
| 48 |  | 50 | 112 |  | $\frac{112}{2} \times\left(\frac{112}{2}-50\right)$ | $=$ |
| 15 | 8 | 17 |  | 60 |  | 60 |
| 21 |  | 29 | 70 | 210 | $=$ |  |
|  | 12 | 37 |  | 210 | $=$ |  |

(b) Write an expression for the area of a right-angled triangle in terms of $P$ and $w$.
(c)


Use your expression from part (b) to find the area of this triangle.
$\qquad$

Question 4 is printed on the next page.

4 (a)


This is a rhombus.
Use Question 3(b) to write down an expression for the area of this rhombus in terms of $P$ and $w$.
(b) Use your expression from part (a) to find the area of this rhombus when $w=41$ and $b=40$.

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