

GCE

Mathematics

Unit 4737: Decision Mathematics 2

Advanced GCE

Mark Scheme for June 2018

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This mark scheme is published as an aid to teachers and students, to indicate the requirements of the examination. It shows the basis on which marks were awarded by examiners. It does not indicate the details of the discussions which took place at an examiners' meeting before marking commenced.

All examiners are instructed that alternative correct answers and unexpected approaches in candidates' scripts must be given marks that fairly reflect the relevant knowledge and skills demonstrated.

Mark schemes should be read in conjunction with the published question papers and the report on the examination.

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Annotations, (including abbreviations), including those used in scoris, which are used when marking.

Annotation in scoris	Meaning
√and ×	
BOD	Benefit of doubt
FT	Follow through
ISW	Ignore subsequent working
M0, M1	Method mark awarded 0, 1
A0, A1	Accuracy mark awarded 0, 1
B0, B1	Independent mark awarded 0, 1
SC	Special case
۸	Omission sign
MR	Misread
Highlighting	

Other abbreviations in mark scheme	Meaning
M1 dep*	Method mark dependent on a previous mark, indicated by *
сао	Correct answer only
oe	Or equivalent
rot	Rounded or truncated
soi	Seen or implied
www	Without wrong working

Subject specific instructions for this question paper

a Annotations should be used whenever appropriate during your marking.

The A, M and B annotations must be used on your standardisation scripts for responses that are not awarded either 0 or full marks. It is vital that you annotate standardisation scripts fully to show how the marks have been awarded.

For subsequent marking you must make it clear how you have arrived at the mark you have awarded.

b An element of professional judgement is required in the marking of any written paper. Remember that the mark scheme is designed to assist in marking incorrect solutions. Correct *solutions* leading to correct answers are awarded full marks but work must not be judged on the answer alone, and answers that are given in the question, especially, must be validly obtained; key steps in the working must always be looked at and anything unfamiliar must be investigated thoroughly.

Correct but unfamiliar or unexpected methods are often signalled by a correct result following an *apparently* incorrect method. Such work must be carefully assessed. When a candidate adopts a method which does not correspond to the mark scheme, award marks according to the spirit of the basic scheme; if you are in any doubt whatsoever (especially if several marks or candidates are involved) you should contact your Team Leader.

c The following types of marks are available.

Μ

A suitable method has been selected and *applied* in a manner which shows that the method is essentially understood. Method marks are not usually lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, eg by substituting the relevant quantities into the formula. In some cases the nature of the errors allowed for the award of an M mark may be specified.

Α

Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated Method mark is earned (or implied). Therefore M0 A1 cannot ever be awarded.

В

Mark for a correct result or statement independent of Method marks.

Unless otherwise indicated, marks once gained cannot subsequently be lost, eg wrong working following a correct form of answer is ignored. Sometimes this is reinforced in the mark scheme by the abbreviation isw. However, this would not apply to a case where a candidate passes through the correct answer as part of a wrong argument.

- d When a part of a question has two or more 'method' steps, the M marks are in principle independent unless the scheme specifically says otherwise; and similarly where there are several B marks allocated. (The notation 'dep *' is used to indicate that a particular mark is dependent on an earlier, asterisked, mark in the scheme.) Of course, in practice it may happen that when a candidate has once gone wrong in a part of a question, the work from there on is worthless so that no more marks can sensibly be given. On the other hand, when two or more steps are successfully run together by the candidate, the earlier marks are implied and full credit must be given.
- e The abbreviation ft implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, A and B marks are given for correct work only differences in notation are of course permitted. A (accuracy) marks are not given for answers obtained from incorrect working. When A or B marks are awarded for work at an intermediate stage of a solution, there may be various alternatives that are equally acceptable. In such cases, exactly what is acceptable will be detailed in the mark scheme rationale. If this is not the case please consult your Team Leader.

Sometimes the answer to one part of a question is used in a later part of the same question. In this case, A marks will often be 'follow through'. In such cases you must ensure that you refer back to the answer of the previous part question even if this is not shown within the image zone. You may find it easier to mark follow through questions candidate-by-candidate rather than question-by-question.

- f Wrong or missing units in an answer should not lead to the loss of a mark unless the scheme specifically indicates otherwise. Candidates are expected to give numerical answers to an appropriate degree of accuracy, with 3 significant figures often being the norm. Small variations in the degree of accuracy to which an answer is given (e.g. 2 or 4 significant figures where 3 is expected) should not normally be penalised, while answers which are grossly over- or under-specified should normally result in the loss of a mark. The situation regarding any particular cases where the accuracy of the answer may be a marking issue should be detailed in the mark scheme rationale. If in doubt, contact your Team Leader.
- g Rules for replaced work

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If a candidate attempts a question more than once, and indicates which attempt he/she wishes to be marked, then examiners should do as the candidate requests.

If there are two or more attempts at a question which have not been crossed out, examiners should mark what appears to be the last (complete) attempt and ignore the others.

NB Follow these maths-specific instructions rather than those in the assessor handbook.

h For a *genuine* misreading (of numbers or symbols) which is such that the object and the difficulty of the question remain unaltered, mark according to the scheme but following through from the candidate's data. A penalty is then applied; 1 mark is generally appropriate, though this may differ for some units. This is achieved by withholding one A mark in the question.

Note that a miscopy of the candidate's own working is not a misread but an accuracy error.

Question	Answer/Indicative content	Mark	Guidance
1 (i)	$(A) \bullet \bullet (1)$ $(B) \bullet \bullet (2)$		For reference: (1) = carrot and houmous, (2) = cheddar and pickle, (3) = chicken and stuffing, (4) = cream cheese, (5) = crab
	$(C) \bullet \bullet (3)$ $(D) \bullet \bullet (4)$	B1	Arcs A-1, C-4 and D-3 (and no other arcs) Must be in the space for (i)
	(E) • • (5)	[1]	
(ii)	(E) = (1) – (A) = (4) – (C) = (2) (A) • • •(1)	B1	This alternating path in this order (accept any notation)
	$(B) \bullet (2)$ $(C) \bullet (3)$	B1	This matching drawn Must be in the space for (ii)
	(D) • (4) (E) • (5)		
		[2]	

Question	Answer/Indicative content	Mark	Guidance
(iii)	(5) = (D) - (3) = (B)	B1	This alternating path in this order (accept any notation)
	(A) = (4) (B) = (3) (C) = (2) (D) = (5) (E) = (1)	B1 [2]	This matching listed Accept any notation. Must be in the space for (iii)
(iv)	$(A) \bullet (1) \\ (B) \bullet (2) \\ (C) \bullet (3) \\ (D) \bullet (4) \\ (E) \bullet (5)$	B1	This complete matching drawn Must be in the space for (iv)

(Question		Answer/Indicative content	Mark	Guidance
2	(i)		The minimum flow out of A is $(2 + 3 =) 5$	B1	Using flow 'out of A' or 'AC and AD' and using '5' or '2 and 3'
			AC must be at least 2 and AD must be at least 3		
	<>			[1] D1	
	(11)		Flow in FT = flow in CF = flow in AC = 2 (from part (1))	BI	Making the connection between FT and AC and using 2
	(:::	(-)			
	(111)	(a)	$(1, 5) \xrightarrow{5} A \xrightarrow{(2, 4)} 2 C \xrightarrow{(1, 5)} 2 \xrightarrow{5} F \xrightarrow{(2, 4)} 3 \xrightarrow{(2, 6)} 5 \xrightarrow{5} T$		
			$(1, 6) \begin{array}{ c c } (1, 6) \end{array} \xrightarrow{(2, 3)} 2 \xrightarrow{(2, 4)} 2 \xrightarrow{E} \xrightarrow{(1, 5)} 2 \xrightarrow{G} \xrightarrow{(1, 2)} 2$	B1	This flow indicated in an appropriate way
		(b)		L_J	
			$s \xrightarrow{0 \uparrow \downarrow 4} a \xrightarrow{2} 0 \uparrow \downarrow 3 \xrightarrow{2} 0 \xrightarrow{2} 0 \xrightarrow{3} 1 \xrightarrow{F} 0 \uparrow \downarrow 2$ $s \xrightarrow{3 \uparrow \downarrow 2} a \xrightarrow{1 \uparrow \downarrow 0} 2 \xrightarrow{E} \xrightarrow{3} 0 \xrightarrow{f} 0 \xrightarrow{f} 0 \uparrow \downarrow 2$ $g \xrightarrow{1 \uparrow \downarrow 0} 2 \xrightarrow{E} \xrightarrow{3} 0 \xrightarrow{f} 0 \xrightarrow{f} 0 \xrightarrow{f} 1$	M1 A1	At least one correct pair (e.g. 0, 4) before augmenting Allow all directions reversed, assume a blank means 0 All correct
		(c)	Values augmented <u>on diagram</u> (<i>S</i> to <i>T</i> subtract 1, <i>T</i> to <i>S</i> add 1) Augmented route <i>SBDT</i>	B1 B1	Values augmented for their route This route written (or in reverse) Accept arcs written provided they are given in the correct order, with no extra arcs
		(d)	Cut: $\{S, B, E, G\}, \{A, C, D, F, T\}$	B1 [5]	Cut through arcs <i>SA</i> , <i>BD</i> and <i>GT</i> described in any way If no written answer allow cut drawn on diagram, provided it is obvious

Question	Answer/Indicative content	Mark	Guidance
3 (i)	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	B1 B1 [2]	Mark final attempt only Convert from minimisation to maximisation (e.g. subtract values from 1000) to give non-negative values Reduce entries to single figures (by dividing by 100) Or equivalent by reducing and then converting
(ii)	Rows reduced N P E B (1) 0 4 8 8 (2) 0 3 5 6 (3) 0 1 2 4 (4) 0 7 6 8 Cols reduced N P E B (1) 0 3 6 4 (2) 0 2 3 2 (3) 0 0 0 0 (4) 0 6 4 4	M1 A1 B1	Reducing each row (question says to reduce rows first, but allow if columns are reduced first instead) Need to see a 0 in each row (or a 0 in each column), condone negative entries if seen, FT (their) answer to (i) Achieving this reduced cost matrix Allow scaled by 100 Evidence of covering May be implied from augmenting
	Augment by 2 N P E B (1) 0 1 4 2 (2) 0 0 1 0 (3) 2 0 0 0 (4) 0 4 2 2 Augment by 1 N P E B (1) 0 0 3 1 (2) 1 0 1 0 (3) 3 0 0 0 (4) 0 3 1 1	M1 A1	Augmenting by least uncovered value Need to see at least one cell 'of each type' augmented correctly Using a second augmentation to achieve this final matrix (or scaled by 100) after exactly two augmentations
		[5]	

(Question	Answer/Indicative content	Mark	Guidance
	(iii)	Event 1 = posters		1 = P
		Event $2 = $ on buses	B1	2 = B
		Event $3 = \text{emails}$		3 = E
		Event $4 =$ newspapers		4 = N
		Total number of people expected $= 2100$	B1 [2]	2100 (not 21)
	(iv)	Adding 80 to each of these gives the same returns as for advertising on buses, so the solution would be the same (except	B1	Evidence that the column entries differ from the given ones by a
		that event $2 - \text{leaflet dron}$		Reducing columns would be the same as for the original values
		that event 2 – fearier drop)	[1]	Reducing columns would be the same as for the original values

(Question		Answer/Indicative content							Mark		Guid	lance		
4	(i)	(a)	Мауа		B1	This table with row a	and column la	ubels (A, D, E	and B, F, H)						
					В	F	Н	row min			Need not show row r	ninima and co	ol maxima		
				А	-1	-3	6	-3	\leftarrow						
			Leo	D	1	-2	-4	-4		B1	Play-safe for $Leo = A$	A			
				Е	2	-1	-4	-4							
				col max	2	-1	6		I	M1	Calculating column r	naxima (or eo	quivalent)		
					•	\uparrow		-			May be implied from	a correct pla	y-safe for Ma	aya	
				Plav-safe for	Leo A		Play-safe	e for Mava F	7	A1	Play-safe for Maya =	F			
		(b)	Maya	would win 3	points		ŷ			B1 ft	3 (follow through the	eir claimed pl	ay-safe for Le	eo)	
		(c)	Leo w	ould play ca	rd E					B1 ft	E (follow through the	eir claimed pl	ay-safe for M	laya)	
										[6]			•	•	
	(ii)	(a)	Using	the five colu	ımns B, C	C, F, G, H	l row min	ima for rows	А,	B1	Row min values sam	e as before			
			D, E a	ure still -3, -4	, -4 so Le	o's play-	safe is sti	ll A			A: -1, -1, -3, -3, $6 \Rightarrow -3$; D: 1,0,-2,-3	,-4 ⇒ -4; E: 2	$2,0,-1,-2,-4 \Rightarrow$	-4
			This r	nakes no diff	erence to	Leo's pl	ay-safe c	hoice (as give	en)						
		(b)	Cards	B, C and H						B1	B, C, H (cao)	B, C, H (cao)			
										[2]					
	(iii)		B bec	ause it is play	y-safe					B1	Least loss for Maya ((lose 2 instead	d of 6) in wor	st case	
			F beca	ause she wins	s with fou	r of the f	ive possi	bilities		B1	4 negative values in o	column F, mo	ore than B or I	H (in the 5	
			** 1	· · ·							remaining columns o	of original tab	le)		
			H bec 3)	ause it gives	the greate	est possit	ole gain (6	5 instead of 4	or	BI	But not using col tota	al or mean (11	any of the th	ree parts)	
											Pay-off for Maya	В	F	Н	
											A	1	3	-6	
											С	-1	3	-5	
											D	-1	2	4	
											E	-2	1	4	
											G	4	-6	6	
											Min for Maya	-2	-6	-6	

Question		on			Answe	r/Indicative conten	ıt	Mark	Guidance
5	(i)			~					
			Stage	State	Action	Working	Suboptimal		
				0	0	4	maximin		
			3	0	0	4	4		
				1	0	3	3		
			2	0	0	$\min(2, 4) = 2$		M1	4 and 3 transferred (three times each) to working column stage 2
				1	1	$\min(4, 3) = 3$ $\min(2, 4) = 3$	3		correctly
				1	0	$\min(3, 4) = 3$ $\min(2, 3) = 2$	3	M1	Their minima calculated in working column
				2	1	$\min(2, 3) = 2$ $\min(5, 4) = 4$	<u> </u>	A1	Suboptimal maximin values and working column correct for stage
				2	1	$\min(3, 4) = 4$ $\min(2, 3) = 2$	-		2 (dependent on first two M marks)
			1	0	0	$\min(2, 3) = 2$			
			-	Ŭ	1	$\min(2, 3) = 3$	3	M1	Using their working values to calculate suboptimal maximin values
				1	1	$\min(2, 3) = 2$	-		for stage 1 (their 3, 2 in final column)
					2	$\min(2, 4) = 2$	2		
			0	0	0	min $(4, 3) = 3$	3	A1ft	Using their working values to calculate suboptimal maximin value
					1	$\min(3, 2) = 2$			for stage 0 (their 3 in final column)
			Maximi	n route:	(0; 0) - (1)	1; 0) - (2; 1) - (3; 0)	-(4;0)	B1	This route written in this form, including $(0; 0)$ and $(4; 0)$
	(::)		(0, 0)	(1, 0) 1	! - 1-4	(1, 0) + (2, 0)	1) 1, 1, . 5	[6]	
	(11)		(0; 0) to $(2; 1)$ to	(1; 0) h	as weight	4 $(1; 0) to (2;$ 3 $(2; 0) to (4;$	1) has weight 5	BIII	Arc weights correct (it their arcs)
			(2, 1) to Minimu	(3, 0) If m of 4	5 3 4 is 3	3 (3, 0) 10 (4, 8 – min weight on th	o) has weight 4	M1	Using their arc weights to calculate min (their 3)
			This is a	rreater th	an (or ed	(1) = 1 (1)	or all other routes	A1	This is the maximum of all the route mins
			No othe	r route g	ives a lar	ger minimum			
						0		[3]	
	(iii)	(a)	Maximu	m path				B1	Maximising, longest path, greatest total weight, or equivalent
		(b)	Route: (0; 0) – (1; 0) - (2)	(1) - (3; 0) - (4; 0)		B1	This route written in this form, including $(0; 0)$ and $(4; 0)$, (cao)
		(c)	4+5+3+	4 = 16, 1	no other re	oute gives a larger to	otal	B1	(Their) 16 or (their) 4+5+3+4 and reference to maximum
								[3]	

	Questi	on	Answer/Indicative content	Mark	Guidance					
6	(i)		Property 1: two opposing teams or players	B1	Explaining two-person					
					('two players' or 'two teams' or equivalent)					
			Property 2: what one player gains the other loses	B1	Explaining zero-sum					
			Property 3: play simultaneously, rather than taking turns	B1	Simultaneous play					
					Do not know what the other side will do when choices are made					
				[3]						
	(ii)		Val should not play in the final because	M1	Val or V					
			for <u>each</u> topic Val's score is lower than Wesley's	A1	Dominance $(W > V)$ in <u>each</u> column (or shown numerically)					
					Wesley's score is <u>always</u> better than Val's					
					V 2 4 1 4					
					W 3 5 2 6					
				[2]						
	(iii)		Famous faces = $3 + 2p$	M1	Any correct expression using U and W or U and V, need not be					
					simplified but must have p as the only variable					
			Films = 5 - 2p		U and W U and V					
					i.e. famous faces $5p + 3(1 - p)$ or $3 + 2p$ $5p + 2(1 - p)$ or $2 + 3p$					
			Food = $2 + 5p$		films $3p + 5(1 - p)$ or $5 - 2p$ $3p + 4(1 - p)$ or $4 - p$					
					food $7p + 2(1 - p)$ or $2 + 5p$ $7p + (1 - p)$ or $1 + 6p$					
			Football = $6 - 3p$		football $3p + 6(1 - p)$ or $6 - 3p$ $3p + 4(1 - p)$ or $4 - p$					
				241						
				MI	Any correct expression, for U and W $\underline{\text{or}}$ U and V, in the form $a+bp$					
				A 1 C						
				AIft	All four correct and simplified, it their row rejected from part (1)					
				[3]						

Question	Answer/Indicative content	Mark	Guidance
(iv)		B1 M1 A1 ft	Horizontally 0 to 1 fills at least half the width <u>and</u> vertical scale Four lines that cut $p = 1$ at 5, 3, 7, 3 (allow dominated line missing) Lines cut $p = 0$ at their <i>a</i> values from part (iii) (or equivalent, if not simplified)
	Value of $p = 0.5$	B1 [4]	0.5 (cao)
(v)	M m p q r s t u v w RHS		Need not label rows or columns and rows/columns may be in any order
	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	B1	Objective row 1 -1 0 0 0 0 in simplex tableau
	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	B1	Four constraint rows or written as inequalities $(m \le 5p + 2q + 3q \text{ etc.})$ or equations with slock $(m = 5p = 2q = 3r + s = 0 \text{ etc.})$
	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	B1 B1	Appropriate use of slack ($m = 5p = 2q = 5r + s = 0$ etc.) $p + q + r \le 1$ or as an equation with slack (in tableau or formulation)
		[4]	If a candidate uses $p + q + r = 1$ to eliminate one of the variables they can get at most B1 B0 B1 B0 because their simplex will not be able to be used to solve the problem

Que	estion	Answer/Indicative content	Mark	Guidance
7	(i)	H 10 30 60 70		For reference: A(20), B(15), C(20), D(10), E(10), F(20), G(50), H(20), I(10), J(20), K(20), L(30), M(10), N(5)
		$\begin{array}{c} F \\ B \\ 12030 \\ 4050 \end{array}$		Consistent but incorrect use of boxes can get at most M1, M1
		0 0 A 20 20 10 10 10 100 105 105 105 105 105 105 1	M1	Dealing with a merge on forward pass (e.g. 20 where B, D and dummy merge), largest value at merge on forwards pass
		E 20 20 G 70 70 K M 10 20 90 90	M1	Dealing with merge of dummies on backwards pass, smallest value at merge on backwards pass
		Ι	A1	All correct
			[3]	
	(ii)	e.g.		
		B B E E H H H H H I L L L L L I N	B1	Either activities B and D or activities C and E are completed by time
				20 (when A finishes)
		A A A A A G G G G G G G G K K K	B1	Activities B, C, D, E, H, I, L, M, N are done by the two people
				and none of A, F, G, J, K
			B1	M starts at time 110 and N starts at time 120
			B1	Bottom two rows: A followed by F, G or G, F with J after F and K
				after G and all completed at time 110
			[4]	
	(iii)	Version 1: 140 (minutes)	B1	Time does not change
		Version 2: 140 (minutes)	B1	Reduced by 15 (minutes)
			[2]	

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