

## **INSTRUCTIONS TO CANDIDATES**

- Write your name, centre number and candidate number in the boxes above. Please write clearly and in capital letters.
- Use black ink. HB pencil may be used for graphs and diagrams only.
- Answer **all** the questions.
- Read each question carefully. Make sure you know what you have to do before starting your answer.
- Your answers should be supported with appropriate working. Marks may be given for a correct method even if the answer is incorrect.
- Write your answer to each question in the space provided. Additional paper may be used if necessary but you must clearly show your candidate number, centre number and question number(s).
- Do **not** write in the bar codes.

# INFORMATION FOR CANDIDATES

- The number of marks is given in brackets [] at the end of each question or part question.
- Quality of written communication will be assessed in questions marked with an asterisk (\*).
- The total number of marks for this paper is **90**.
- This document consists of **16** pages. Any blank pages are indicated.



2

#### Formulae Sheet: Higher Tier









Volume of sphere =  $\frac{4}{3}\pi r^3$ 

Surface area of sphere =  $4\pi r^2$ 

Volume of prism = (area of cross-section) × length





Volume of cone =  $\frac{1}{3}\pi r^2 h$ Curved surface area of cone =  $\pi rl$ 

#### The Quadratic Equation

The solutions of  $ax^2 + bx + c = 0$ , where  $a \neq 0$ , are given by

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

#### PLEASE DO NOT WRITE ON THIS PAGE

## Answer **all** the questions.

1 (a) Fill in the missing fractions, decimals and percentages in the table below. Give answers in their simplest forms. The top row has been done for you.

Fraction	Decimal	Percentage
$\frac{1}{4}$	0.25	25%
7 20		
	0.64	
		44%

[4]

(b) Find the missing number.



(c) Find a number that is bigger than  $\frac{1}{3}$  but smaller than  $\frac{1}{2}$ .

(c) .....[2]

[1]

2\* The tiling pattern below is made from eight congruent squares and four congruent hexagons. Each hexagon has one line of symmetry.



**Calculate** all six angles of hexagon ABCDEF. Give a geometrical reason for each step in your working.

- 3 (a) Find the missing numbers in this sequence.
  - 1, 3, 6, ....., 15, .....
  - (b) Show that 2n 1 is **not** an expression for the *n*th term of the sequence in part (a).

(c) The *n*th term of another sequence is 4n - 2.

How many terms of this sequence are smaller than 200?

(c) .....[4]

[2]

4 (a) Share £60 in the ratio 8:7.

(a)	£,	£	[2]
<b>x</b> - <b>y</b>	,		

- (b) The ratio of red sweets to black sweets in a bag is 3:2. There are only red sweets and black sweets in the bag.
  - (i) What fraction of the sweets in the bag are red?

(b)(i)		[1]
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(ii) Kirsty opens the bag of sweets and eats 5 black sweets. This leaves only one black sweet in the bag.

What is the ratio of red sweets to black sweets now?

(ii) ......[3]

5 (a) Solve.

7(x+2) = 9x - 1

(a) ......[3]

(b) Make *t* the subject of the following formula.

v = u + at

(b) .....[2]

6 The lengths of the sides in a right angled triangle are in the ratio 3:4:5.



Not to scale

Calculate the size of the smallest angle in the triangle.

.....° [3]

7 The point (4, 2) lies on the circumference of a circle centre the origin.



(a) Find the coordinates of the other end of the diameter that passes through (4, 2).

(a) (.....) [2]

(b) Calculate the radius of the circle.

(b) ..... units [3]

(c) Write down the equation of the circle.

(c) ......[2]

8 (a) The shape below is made from a semicircle and a triangle PQR. The triangle is isosceles and right-angled. PQ is the diameter of the semicircle. PQ = 8 cm.



Calculate the area of the shape.

(a) ..... cm<sup>2</sup> [5]

(b) The cross-section of a prism has area  $81 \text{ cm}^2$ . The volume of the prism is  $350 \text{ cm}^3$ .

Calculate the length of the prism.

(b) ..... cm [2]

Turn over

9 (a) Complete the table for  $y = x^3 - 2x^2$ .

x	-1	-0.5	0	0.5	1	1.5	2	2.5	3	
у		-0.625		-0.375		-1.125			9	
										[2]

(b) Draw the graph of  $y = x^3 - 2x^2$  for x between -1 and 3.



[2]

10 (a) Expand and simplify.

$$(6x-1)(x+3)$$

(a) .....[3]

(b) Solve.

 $2x^2 - x - 6 = 0$ 

(b) .....[4]

**11** A pair of shoes costs £69. This includes VAT at 20%.

What was the cost of the shoes before VAT was added on?

£.....[2]

Turn over

12 The diagram below shows triangle ABC, which is right-angled at B. AB = 2 BC.M is the midpoint of AB.

N is on AC such that MN is perpendicular to AC. P is on AC such that BP is parallel to MN.



(a)\* Prove that triangles AMN and BPC are congruent.

 	[4]

(b) Find the ratio of the area of triangle AMN to the area of triangle ABP.

(b) ......[2]

(c) What is the ratio of the area of triangle AMN to the area of triangle ABC?

(c) .....[1]

- **13** *y* is directly proportional to the square of *h*. When h = 2, y = 12.
  - (a) Find y when h = 4.

(b) Find *h* when y = 75.

(a) .....[3]

(b) ......[2]

Point P is at the top of a hill.
Points A and B lie on horizontal ground.
ABG is a straight line, with G vertically below P.
P is observed from points A and B.
AB = 100 m. Angle PAB = 26°; angle PBG = 31°.



Calculate the height of the hill, PG.

..... m [6]

**15** A cube has sides 9 cm long.

A pyramid at **each** vertex of the cube is removed to make a new solid.



The diagrams below show how a pyramid is removed from the cube. L, M and N are midpoints of edges of the cube. V is a vertex of the cube. All the pyramids removed are congruent.



Find the volume of the new solid.

Turn over

**16** Solve these simultaneous equations.

$$y = x^2 - 9x + 7$$
$$y = 3 - 5x$$

## **END OF QUESTION PAPER**



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