## Thursday 16 June 2016 - Afternoon

## GCSE METHODS IN MATHEMATICS

B392/02 Methods in Mathematics 2 (Higher Tier)

Candidates answer on the Question Paper.
OCR supplied materials:
None
Other materials required:

- Scientific or graphical calculator
- Geometrical instruments
- Tracing paper (optional)

Duration: 2 hours


| Candidate <br> forename | Candidate <br> surname |  |
| :--- | :--- | :--- | :--- |


| Centre number |  |  |  |  |  | Candidate number |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

## INSTRUCTIONS TO CANDIDATES

- Write your name, centre number and candidate number in the boxes above. Please write clearly and in capital letters.
- Use black ink. HB pencil may be used for graphs and diagrams only.
- Answer all the questions.
- Read each question carefully. Make sure you know what you have to do before starting your answer.
- Your answers should be supported with appropriate working. Marks may be given for a correct method even if the answer is incorrect.
- Write your answer to each question in the space provided. Additional paper may be used if necessary but you must clearly show your candidate number, centre number and question number(s).
- Do not write in the bar codes.


## INFORMATION FOR CANDIDATES

- The number of marks is given in brackets [ ] at the end of each question or part question.
- Quality of written communication will be assessed in questions marked with an asterisk (*).
- The total number of marks for this paper is 90 .
- This document consists of 16 pages. Any blank pages are indicated.



## Formulae Sheet: Higher Tier

Area of trapezium $=\frac{1}{2}(a+b) h$


Volume of prism $=($ area of cross-section $) \times$ length

In any triangle $A B C$
Sine rule $\quad \frac{a}{\sin A}=\frac{b}{\sin B}=\frac{c}{\sin C}$

Cosine rule $a^{2}=b^{2}+c^{2}-2 b c \cos A$


Area of triangle $=\frac{1}{2} a b \sin C$

Volume of sphere $=\frac{4}{3} \pi r^{3}$
Surface area of sphere $=4 \pi r^{2}$


Volume of cone $=\frac{1}{3} \pi r^{2} h$
Curved surface area of cone $=\pi r l$


## The Quadratic Equation

The solutions of $a x^{2}+b x+c=0$,
where $a \neq 0$, are given by
$x=\frac{-b \pm \sqrt{\left(b^{2}-4 a c\right)}}{2 a}$

Answer all the questions.
1 (a) Fill in the missing fractions, decimals and percentages in the table below.
Give answers in their simplest forms.
The top row has been done for you.

| Fraction | Decimal | Percentage |
| :---: | :---: | :---: |
| $\frac{1}{4}$ | 0.25 | $25 \%$ |
| $\frac{7}{20}$ | 0.64 |  |
|  |  | $44 \%$ |

(b) Find the missing number.

(c) Find a number that is bigger than $\frac{1}{3}$ but smaller than $\frac{1}{2}$.
(c)

2* The tiling pattern below is made from eight congruent squares and four congruent hexagons. Each hexagon has one line of symmetry.


Calculate all six angles of hexagon ABCDEF. Give a geometrical reason for each step in your working.
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

3 (a) Find the missing numbers in this sequence.
1, 3,6 , 15,
(b) Show that $2 n-1$ is not an expression for the $n$th term of the sequence in part (a).
$\qquad$
$\qquad$
$\qquad$
(c) The $n$th term of another sequence is $4 n-2$.

How many terms of this sequence are smaller than 200 ?
(c)

4 (a) Share $£ 60$ in the ratio 8:7.
(a) $£$
£
(b) The ratio of red sweets to black sweets in a bag is 3:2. There are only red sweets and black sweets in the bag.
(i) What fraction of the sweets in the bag are red?

> (b)(i)
(ii) Kirsty opens the bag of sweets and eats 5 black sweets. This leaves only one black sweet in the bag.

What is the ratio of red sweets to black sweets now?
(ii)

5 (a) Solve.

$$
7(x+2)=9 x-1
$$

(a)
(b) Make $t$ the subject of the following formula.

$$
v=u+a t
$$

(b)

6 The lengths of the sides in a right angled triangle are in the ratio $3: 4: 5$.


Not to scale

Calculate the size of the smallest angle in the triangle.

7 The point $(4,2)$ lies on the circumference of a circle centre the origin.

(a) Find the coordinates of the other end of the diameter that passes through (4, 2).
(a) (........................ , .........................)
[2]
(b) Calculate the radius of the circle.
(b)
units [3]
(c) Write down the equation of the circle.
(c)

8 (a) The shape below is made from a semicircle and a triangle PQR.
The triangle is isosceles and right-angled.
$P Q$ is the diameter of the semicircle.
$P Q=8 \mathrm{~cm}$.


Calculate the area of the shape.
(a)
$\mathrm{cm}^{2}$
(b) The cross-section of a prism has area $81 \mathrm{~cm}^{2}$. The volume of the prism is $350 \mathrm{~cm}^{3}$.

Calculate the length of the prism.
(b)
cm [2]

9 (a) Complete the table for $y=x^{3}-2 x^{2}$.

| $x$ | -1 | -0.5 | 0 | 0.5 | 1 | 1.5 | 2 | 2.5 | 3 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $y$ |  | -0.625 |  | -0.375 |  | -1.125 |  |  | 9 |

(b) Draw the graph of $y=x^{3}-2 x^{2}$ for $x$ between -1 and 3 .


10 (a) Expand and simplify.

$$
(6 x-1)(x+3)
$$

(a)
(b) Solve.

$$
2 x^{2}-x-6=0
$$

(b)

11 A pair of shoes costs £69. This includes VAT at 20\%.
What was the cost of the shoes before VAT was added on?

12 The diagram below shows triangle $A B C$, which is right-angled at $B$.
$A B=2 B C$.
$M$ is the midpoint of $A B$.
$N$ is on $A C$ such that $M N$ is perpendicular to $A C$.
$P$ is on $A C$ such that $B P$ is parallel to $M N$.

(a)* Prove that triangles AMN and BPC are congruent.
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
(b) Find the ratio of the area of triangle AMN to the area of triangle ABP.
(b) :
(c) What is the ratio of the area of triangle $A M N$ to the area of triangle $A B C$ ?
$13 y$ is directly proportional to the square of $h$. When $h=2, y=12$.
(a) Find $y$ when $h=4$.
(a)
[3]
(b) Find $h$ when $y=75$.
(b)

14 Point P is at the top of a hill.
Points A and B lie on horizontal ground.
ABG is a straight line, with $G$ vertically below $P$.
$P$ is observed from points $A$ and $B$.
$\mathrm{AB}=100 \mathrm{~m}$. Angle $\mathrm{PAB}=26^{\circ}$; angle $\mathrm{PBG}=31^{\circ}$.


Not to scale

Calculate the height of the hill, PG.

15 A cube has sides 9 cm long.
A pyramid at each vertex of the cube is removed to make a new solid.


The diagrams below show how a pyramid is removed from the cube.
$\mathrm{L}, \mathrm{M}$ and N are midpoints of edges of the cube. V is a vertex of the cube.
All the pyramids removed are congruent.


Find the volume of the new solid.
$\qquad$ $\mathrm{cm}^{3}[6]$

16 Solve these simultaneous equations.

$$
\begin{aligned}
& y=x^{2}-9 x+7 \\
& y=3-5 x
\end{aligned}
$$

$$
x=
$$

$\qquad$
$y=$

END OF QUESTION PAPER

## OCR

## Oxford Cambridge and RSA

## Copyright Information

OCR is committed to seeking permission to reproduce all third-party content that it uses in its assessment materials. OCR has attempted to identify and contact all copyright holders whose work is used in this paper. To avoid the issue of disclosure of answer-related information to candidates, all copyright acknowledgements are reproduced in the OCR Copyright Acknowledgements Booklet. This is produced for each series of examinations and is freely available to download from our public website (www.ocr.org.uk) after the live examination series. If OCR has unwittingly failed to correctly acknowledge or clear any third-party content in this assessment material, OCR will be happy to correct its mistake at the earliest possible opportunity.
For queries or further information please contact the Copyright Team, First Floor, 9 Hills Road, Cambridge CB2 1GE.
OCR is part of the Cambridge Assessment Group; Cambridge Assessment is the brand name of University of Cambridge Local Examinations Syndicate (UCLES), which is itself a department of the University of Cambridge.
© OCR 2016

