## GCSE

# Methods in Mathematics (Pilot) 

Unit B392/02: Higher Tier
General Certificate of Secondary Education

## Mark Scheme for June 2016

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This mark scheme is published as an aid to teachers and students, to indicate the requirements of the examination. It shows the basis on which marks were awarded by examiners. It does not indicate the details of the discussions which took place at an examiners' meeting before marking commenced.

All examiners are instructed that alternative correct answers and unexpected approaches in candidates' scripts must be given marks that fairly reflect the relevant knowledge and skills demonstrated.

Mark schemes should be read in conjunction with the published question papers and the report on the examination.

OCR will not enter into any discussion or correspondence in connection with this mark scheme.

Annotations used in the detailed Mark Scheme.

| Annotation | Meaning |
| :---: | :--- |
| Correct |  |
| BOD | Incorrect |
| FT | Benefit of doubt |
| $\boxed{\text { ISW }}$ | Follow through |
| M0 | Ignore subsequent working (after correct answer obtained), provided method has been completed |
| M1 | Method mark awarded 0 |
| M2 | Method mark awarded 1 |
| A1 | Method mark awarded 2 |
| B1 | Accuracy mark awarded 1 |
| B2 | Independent mark awarded 1 |
| MR | Independent mark awarded 2 |
| SC | Misread |
| A | Special case |
| An | Omission sign |

These should be used whenever appropriate during your marking.
The M, A, B, etc annotations must be used on your standardisation scripts for responses that are not awarded either 0 or full marks. It is vital that you annotate these scripts to show how the marks have been awarded.
It is not mandatory to use annotations for any other marking, though you may wish to use them in some circumstances.

## Subject-Specific Marking Instructions

1. M marks are for using a correct method and are not lost for purely numerical errors.

A marks are for an accurate answer and depend on preceding M (method) marks. Therefore M0 A1 cannot be awarded.
B marks are independent of $\mathbf{M}$ (method) marks and are for a correct final answer, a partially correct answer, or a correct intermediate stage. SC marks are for special cases that are worthy of some credit.
2. Unless the answer and marks columns of the mark scheme specify $\mathbf{M}$ and $\mathbf{A}$ marks etc, or the mark scheme is 'banded', then if the correct answer is clearly given and is not from wrong working full marks should be awarded.

Do not award the marks if the answer was obtained from an incorrect method, ie incorrect working is seen and the correct answer clearly follows from it.
3. Where follow through (FT) is indicated in the mark scheme, marks can be awarded where the candidate's work follows correctly from a previous answer whether or not it was correct.

Figures or expressions that are being followed through are sometimes encompassed by single quotation marks after the word their for clarity, eg FT $180 \times$ (their ' 37 ' +16 ), or FT $300-\sqrt{ }\left(\right.$ their ${ }^{\prime} 5^{2}+7^{23}$ ). Answers to part questions which are being followed through are indicated by eg FT $3 \times$ their (a).

For questions with FT available you must ensure that you refer back to the relevant previous answer. You may find it easier to mark these questions candidate by candidate rather than question by question.
4. Where dependent (dep) marks are indicated in the mark scheme, you must check that the candidate has met all the criteria specified for the mark to be awarded.
5. The following abbreviations are commonly found in GCSE Mathematics mark schemes.

- figs 237, for example, means any answer with only these digits. You should ignore leading or trailing zeros and any decimal point eg 237000, 2.37, 2.370, 0.00237 would be acceptable but 23070 or 2374 would not.
- isw means ignore subsequent working after correct answer obtained and applies as a default.
- nfww means not from wrong working.
- oe means or equivalent.
- rot means rounded or truncated.
- seen means that you should award the mark if that number/expression is seen anywhere in the answer space, including the answer line, even if it is not in the method leading to the final answer.
- soi means seen or implied.

6. In questions with no final answer line, make no deductions for wrong work after an acceptable answer (ie isw) unless the mark scheme says otherwise, indicated by the instruction 'mark final answer'.
7. In questions with a final answer line following working space,
(i) if the correct answer is seen in the body of working and the answer given on the answer line is a clear transcription error allow full marks unless the mark scheme says 'mark final answer'. Place the annotation $\checkmark$ next to the correct answer.
(ii) if the correct answer is seen in the body of working but the answer line is blank, allow full marks. Place the annotation $\checkmark$ next to the correct answer.
(iii) if the correct answer is seen in the body of working but a completely different answer is seen on the answer line, then accuracy marks for the answer are lost. Method marks could still be awarded. Use the M0, M1, M2 annotations as appropriate and place the annotation $x$ next to the wrong answer.
8. In questions with a final answer line:
(i) If one answer is provided on the answer line, mark the method that leads to that answer.
(ii) If more than one answer is provided on the answer line and there is a single method provided, award method marks only.
(iii) If more than one answer is provided on the answer line and there is more than one method provided, award zero marks for the question unless the candidate has clearly indicated which method is to be marked.
9. In questions with no final answer line:
(i) If a single response is provided, mark as usual.
(ii) If more than one response is provided, award zero marks for the question unless the candidate has clearly indicated which response is to be marked.
10. When the data of a question is consistently misread in such a way as not to alter the nature or difficulty of the question, please follow the candidate's work and allow follow through for $\mathbf{A}$ and $\mathbf{B}$ marks. Deduct 1 mark from any $\mathbf{A}$ or $\mathbf{B}$ marks earned and record this by using the MR annotation. $\mathbf{M}$ marks are not deducted for misreads.
11. Unless the question asks for an answer to a specific degree of accuracy, always mark at the greatest number of significant figures even if this is rounded or truncated on the answer line. For example, an answer in the mark scheme is 15.75 , which is seen in the working. The candidate then rounds or truncates this to $15.8,15$ or 16 on the answer line. Allow full marks for the 15.75 .
12. Ranges of answers given in the mark scheme are always inclusive.
13. For methods not provided for in the mark scheme give as far as possible equivalent marks for equivalent work. If in doubt, consult your Team Leader.
14. Anything in the mark scheme which is in square brackets [...] is not required for the mark to be earned, but if present it must be correct.

| Question |  | Answer |  |  |  | Marks | Part Marks and Guidance |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | (a) | $\begin{aligned} & \frac{1}{4} \\ & \frac{7}{20} \\ & \frac{16}{2!} \\ & \frac{1}{2} \end{aligned}$ | 1 $\frac{7}{20}$ $\frac{16}{25}$ $\frac{11}{25}$ | 0.25 <br> [0]. 35 <br> 0.64 <br> [0]. 44 | $25 \%$ <br> $35 \%$ <br> 64\% <br> $44 \%$ | 4 | 3 for five correct <br> 2 for three correct <br> 1 for two correct | Condone missing \% signs |
|  | (b) | $\frac{1}{14}$ | $\frac{1}{4}$ |  |  | 1 | Allow 14-1 | Accept 0.071428571.... Allow decimal (rot) in the answer box if acceptable answer seen elsewhere. |
|  | (c) |  | racti | cimal be | $1 / 3$ and $1 / 2$ | 2 | M1 for 0.33 .. and 0.5 or $\frac{1}{2}+\frac{1}{3}$ <br> or correctly converting to fractions with common denominator | Condone correct \% for M1 |


| 2* | ```Angles \(90^{\circ} 270^{\circ} 135^{\circ} 135^{\circ} 45^{\circ} 4^{\circ}\) identified correctly with clear, correct reasons relating to appropriate angles eg \(\mathbf{A}=\mathbf{9 0}^{\mathbf{\circ}}\) (four of these at a point make \(360^{\circ}\) ) \(B=135^{\circ}\) (angles at a point) \(\mathrm{F}=13 \mathbf{1 0}^{\text {o }}\) (equal to B by symmetry) \(\mathrm{D}=\mathbf{2 7 0}\) (angles at a point) \(\mathbf{C = E}=45\) (symmetry and angles of hexagon add up to \(720^{\circ}\) )``` | 5 | 4 for four correct angles with correct reasons that clearly apply to at least two angles or values for all six angles correctly identified with no reasons. <br> 3 for four angles correctly identified with no reasons or three angles with a correct reason that clearly applies to at least one of them. <br> 2 for at least three angles correctly identified <br> 1 for one of the four angles correctly identified <br> Condone use of single letters to identify angles but marks for reasons cannot be awarded for calculations alone. |
| :---: | :---: | :---: | :---: |


| Question |  |  | Answer | Marks | Part Marks and Guidance |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 3 | (a) |  | 10, 21 | 1,1 |  |  |
|  | (b) |  | A correct comparison with justification | 2 | M1 Correct example or statement with no comparison | $\frac{\text { Alt method }}{\text { M1 for }[1 / 2] n^{2}}$ A1 for $\frac{n(n+1)}{2} \neq 2 n-1$ oe |
|  | (c) |  | 50 nfww | 4 | M1 for $4 n-2 \rightarrow 200$ <br> AND <br> M1 for $4 n \rightarrow 202$ <br> AND <br> M1 for $n \rightarrow 50.5$ <br> OR if zero scored SC2 for 50.5 as answer | Alt method <br> M3 for trials including $n=50$ and $n=51$ with correct results <br> OR <br> M2 for trials including $n=50$ or $n=51$ with correct results OR M1 for any correct trial |
| 4 | (a) |  | £32, £28 | 2 | M1 for $60 \div(8+7)$ | Either order |
|  | (b) | (i) | $\frac{3}{5} \text { oe }$ | 1 |  | Must be fraction |
|  |  | (ii) | 9:1 | 3 | M2 for 9 red or ratio 9:6 seen or correct unsimplified ratio using whole numbers ( $9 k: k$ ) <br> OR <br> M1 for 6 black or correct ratio not in integer form | Not 6:9 for M2 eg 18:2 <br> eg 3:0.333[3....] |
| 5 | (a) |  | [ $\mathrm{x}=\mathrm{]} 7.5$ oe | 3 | M1 for $7 x+14$ <br> M1 for getting numbers and $x$ on different sides <br> M1 for correct FT from $\mathrm{kx}=\mathrm{n}$ | Correct numbers and correct x from their equation $k \neq 1$ <br> Max. of M2 for incorrect answer |
|  | (b) |  | $[t=] \frac{v-u}{a} \text { oe }$ | 2 | M1 for $v-u=a t$ oe |  |


| Question |  | Answer | Marks | Part Marks and Guidance |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 6 |  | $36.8 \ldots$ to 36.9 | 3 | M2 for correct inverse trig statement for either angle or 53.1.... <br> OR <br> M1 for $\cos A=\frac{4}{5}$ or $\sin A=\frac{3}{5}$ or $\tan A=\frac{3}{4}$ | Allow 37 (3 marks) or 53 (for M2) with correct working. |
| 7 | (a) | (-4, -2) | 1,1 |  |  |
|  | (b) | 4.47.... | 3 | M2 for $\sqrt{ }\left(4^{2}+2^{2}\right)$ OR <br> M1 for $4^{2}+2^{2}$ or $\sqrt{ }\left(4^{2}-2^{2}\right)$ <br> OR after 0 scored SC1 for answer $\sqrt{80}$ oe | Allow 4.5 or $\sqrt{20}$ or $2 \sqrt{ } 5$ for 3 marks |
|  | (c) | $x^{2}+y^{2}=20$ oe | FT2 | M1 for $x^{2}+y^{2}$ | FT for $\mathrm{x}^{2}+\mathrm{y}^{2}=$ their $\mathrm{r}^{2}$ |
| 8 | (a) | 57.1 to $57.14 \ldots$ or 57 nfww | 5 | B1 for radius $=4 \mathrm{~cm}$ soi <br> M1 for Semicircle $=\frac{\pi(\text { their } 4)^{2}}{2}$ <br> A1 semicircle $=25.1$ to 25.14 .. or 25 or $8 \pi$ <br> M1 for $\frac{8 \times 8}{2}$ oe | May be on diagram <br> 25 without working scores 0 marks |
|  | (b) | 4.3[2.....] | 2 | M1 for $350 \div 81$ |  |


| Question |  | Answer | Marks | Part Marks and Guidance |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 9 | (a) | -3, 0, -1, 0, 3.125 | 2 | B1 for at least two correct |  |
|  | (b) |  | 2 | B1 for at least four points from their table correctly plotted AND B1 for correct smooth curve | Within half a small square <br> Within half a small square BO for multiple or "hairy" curves |
| 10 | (a) | $6 x^{2}+17 x-3$ | 3 | M2 for three of the following terms : $6 x^{2}+18 x-x-3$ <br> OR M1 for two terms | $+17 x$ may count as two terms |
|  | (b) | -1.5, 2 nfww | 4 | M2 for correct factors $(2 x+3)(x-2)$ <br> OR <br> M1 for factors which multiply to give two correct terms in $2 x^{2}-x-6$ <br> AND <br> B1 for each answer | Alternative methods <br> M2 for $\frac{1 \pm \sqrt{49}}{4}$ <br> OR <br> M1 for $\frac{1 \pm \sqrt{1^{2}-4 \times 2 \times(-6)}}{2 \times 2}$ <br> condone 1 error <br> OR <br> M2 for $2\left(x-\frac{1}{4}\right)^{2}-6 \frac{1}{8}=0$ oe <br> OR <br> M1 for $\left(x-\frac{1}{4}\right)^{2}$ |


| Question |  | Answer | Marks | Part Marks and Guidance |  |
| :---: | :--- | :--- | :---: | :---: | :--- | :--- |
| $\mathbf{1 1}$ |  | 57.50 | $\mathbf{2}$ | M1 for $69 \div 1.2$ or 57.5 |  |


| 12 | (a)* | All three equality statements with justifications and correct congruence statement. <br> eg <br> $A M=B C$ [given] <br> Angle BPC = angle ANM [=90ํ] (corresponding) <br> Angle PBC = angle MAN ( $90^{\circ}-$ angle ABP) <br> Triangles are congruent AAS | 4 | 3 for three equality statements with justifications or three equality statements and congruence case relating to their statements <br> 2 for two equality statements with justifications or three equality statements <br> 1 for one equality statement with justification or two equality statements <br> Condone use of $F$ angles, etc. |
| :---: | :---: | :---: | :---: | :---: |


| Question |  | Answer | Marks | Part Marks and Guidance |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 12 | (b) | 1:4 with correct working | 2 | B1 for length scale factor $=2$ or $1 / 2$ soi or area scale factor $=4$ or $1 / 4$ soi | Ratio of 1:2 or 2:1 may relate to length scale factor $=2$ |
|  | (c) | 1:5 | FT1 |  | FT their (b) ie ratio of $a: b(a<b)$ in (b) will give ratio of $\mathrm{a}: \mathrm{a}+\mathrm{b}$ in (c) for FT |
| 13 | (a) | 48 | 3 | M2 for $y=3 h^{2}$ OR $3 \times 4^{2}$ OR <br> M1 for $k=3$ or for $y=k h^{2}$ <br> OR after 0 scored <br> SC1 for $16.97 \ldots$... or $12 \sqrt{ } 2$ |  |
|  | (b) | $[ \pm] 5$ | FT2 | M1 for use of $75=$ their $^{2}{ }^{2}$ oe OR <br> SC1 for answer of 78.125 or for 12.5 from 24 in part (a) | FT from their k |


| Question |  | Answer | Marks | Part Marks and Guidance |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 14 |  | 258.8 to 259.2 | 6 | B1 for $\angle \mathrm{ABP}=149$ or $\angle \mathrm{APB}=5$ soi AND <br> M3 for 502.9... as length of BP rot <br> OR <br> M2 for $\frac{100 \times \sin 26}{\sin \text { their } 5}$ <br> OR <br> M1 for $\frac{100}{\sin \text { their } 5}=\frac{B P}{\sin 26}$ oe <br> AND <br> M1 for theirBPsin31 oe for PG | Alternative method 1 <br> B1 for $\angle A B P=149$ or $\angle A P B=5$ soi AND <br> M3 for 590.9... as length of AP rot <br> OR <br> M2 for $\frac{100 \times \sin \text { their } 149}{\sin \text { their } 5}$ oe <br> OR <br> M1 for $\frac{100}{\sin \text { their } 5}=\frac{A P}{\sin \text { their } 149}$ oe <br> AND <br> M1 for theirAPsin26 oe for PG <br> Alternative method 2 <br> M2 for $B G=\frac{P G}{\tan 31}$ <br> OR <br> M1 for $\tan 31=\frac{\mathrm{PG}}{\mathrm{BG}}$ <br> AND <br> M2 for $A G=\frac{P G}{\tan 26}$ <br> OR <br> M1 for $\tan 26=\frac{P G}{A G}$ <br> AND <br> M1 for $A G-B G=\frac{P G}{\tan 26}-\frac{P G}{\tan 31}$ oe $100=P G \times 0.386 \ldots$ |


| Question |  | Answer | Marks | Part Marks and Guidance |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 15 |  | 607.5 | 6 | M1 for area of base of pyramid $=$ $\frac{1}{2} \times 4.5 \times 4.5$ <br> M1 for volume of pyramid $=$ $\frac{1}{3}$ (their base area) $\times 4.5$ A1 for 15.1875 <br> AND <br> M2 for $9^{3}-8 \times$ their 15.1875 OR M1 for $9^{3}$ or 729 or $8 \times$ their 15.1875 | May be contained within eg $\frac{1}{2} \times 4.5 \times 4.5 \times 4.5$ |
| 16 |  | 2, -7 | 5 | M1 attempt to eliminate y <br> M1 their 3 term quadratic [=0] <br> M1 factorise correctly or other fully correct method <br> B1, B1 for correct answers | Correct is $x^{2}-4 x+4=0$ (allow 1 arithmetic slip) $(x-2)^{2}=0$ <br> Equivalent marks for process that eliminates x |

OCR (Oxford Cambridge and RSA Examinations)
1 Hills Road
Cambridge
CB1 2EU

## OCR Customer Contact Centre

## Education and Learning

Telephone: 01223553998
Facsimile: 01223552627
Email: general.qualifications@ocr.org.uk
www.ocr.org.uk

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Head office
Telephone: 01223552552
Facsimile: 01223552553

