## GCSE

# Methods in Mathematics (Pilot) 

Unit B392/02: Higher Tier
General Certificate of Secondary Education

## Mark Scheme for June 2017

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This mark scheme is published as an aid to teachers and students, to indicate the requirements of the examination. It shows the basis on which marks were awarded by examiners. It does not indicate the details of the discussions which took place at an examiners' meeting before marking commenced.

All examiners are instructed that alternative correct answers and unexpected approaches in candidates' scripts must be given marks that fairly reflect the relevant knowledge and skills demonstrated.

Mark schemes should be read in conjunction with the published question papers and the report on the examination.

OCR will not enter into any discussion or correspondence in connection with this mark scheme.

## Annotations used in the detailed Mark Scheme.

| Annotation | Meaning |
| :---: | :--- |
|  | Correct |
| BOD | Incorrect |
| FT | Benefit of doubt |
| $\boxed{\text { ISW }}$ | Follow through |
| M0 | Ignore subsequent working (after correct answer obtained), provided method has been completed |
| M1 | Method mark awarded 0 |
| M2 | Method mark awarded 1 |
| A1 | Method mark awarded 2 |
| $\mathbf{B 1}$ | Accuracy mark awarded 1 |
| $\mathbf{B 2}$ | Independent mark awarded 1 |
| $\mathbf{M R}$ | Independent mark awarded 2 |
| $\mathbf{S C}$ | Misread |
| $\mathbf{A}$ | Special case |
|  | Omission sign |

## Subject-Specific Marking Instructions

1. $\mathbf{M}$ marks are for using a correct method and are not lost for purely numerical errors.

A marks are for an accurate answer and depend on preceding M (method) marks. Therefore M0 A1 cannot be awarded.
B marks are independent of $\mathbf{M}$ (method) marks and are for a correct final answer, a partially correct answer, or a correct intermediate stage. SC marks are for special cases that are worthy of some credit.
2. Unless the answer and marks columns of the mark scheme specify $\mathbf{M}$ and $\mathbf{A}$ marks etc, or the mark scheme is 'banded', then if the correct answer is clearly given and is not from wrong working full marks should be awarded.

Do not award the marks if the answer was obtained from an incorrect method, ie incorrect working is seen and the correct answer clearly follows from it.
3. Where follow through (FT) is indicated in the mark scheme, marks can be awarded where the candidate's work follows correctly from a previous answer whether or not it was correct.

Figures or expressions that are being followed through are sometimes encompassed by single quotation marks after the word their for clarity, eg FT $180 \times$ (their ' $37^{\prime}+16$ ), or FT $300-\sqrt{ }\left(\right.$ their ${ }^{\prime} 5^{2}+7^{23}$ ). Answers to part questions which are being followed through are indicated by eg FT $3 \times$ their (a).

For questions with FT available you must ensure that you refer back to the relevant previous answer. You may find it easier to mark these questions candidate by candidate rather than question by question.
4. Where dependent (dep) marks are indicated in the mark scheme, you must check that the candidate has met all the criteria specified for the mark to be awarded.
5. The following abbreviations are commonly found in GCSE Mathematics mark schemes.

- figs 237, for example, means any answer with only these digits. You should ignore leading or trailing zeros and any decimal point eg 237000, 2.37, 2.370, 0.00237 would be acceptable but 23070 or 2374 would not.
- isw means ignore subsequent working after correct answer obtained and applies as a default.
- nfww means not from wrong working.
- oe means or equivalent.
- rot means rounded or truncated.
- seen means that you should award the mark if that number/expression is seen anywhere in the answer space, including the answer line, even if it is not in the method leading to the final answer.
- soi means seen or implied.

6. In questions with no final answer line, make no deductions for wrong work after an acceptable answer (ie isw) unless the mark scheme says otherwise, indicated by the instruction 'mark final answer'.
7. In questions with a final answer line following working space,
(i) if the correct answer is seen in the body of working and the answer given on the answer line is a clear transcription error allow full marks unless the mark scheme says 'mark final answer'. Place the annotation $\checkmark$ next to the correct answer.
(ii) if the correct answer is seen in the body of working but the answer line is blank, allow full marks. Place the annotation $\checkmark$ next to the correct answer.
(iii) if the correct answer is seen in the body of working but a completely different answer is seen on the answer line, then accuracy marks for the answer are lost. Method marks could still be awarded. Use the M0, M1, M2 annotations as appropriate and place the annotation $\mathbf{x}$ next to the wrong answer.
8. In questions with a final answer line:
(i) If one answer is provided on the answer line, mark the method that leads to that answer.
(ii) If more than one answer is provided on the answer line and there is a single method provided, award method marks only.
(iii) If more than one answer is provided on the answer line and there is more than one method provided, award zero marks for the question unless the candidate has clearly indicated which method is to be marked.
9. In questions with no final answer line:
(i) If a single response is provided, mark as usual.
(ii) If more than one response is provided, award zero marks for the question unless the candidate has clearly indicated which response is to be marked.
10. When the data of a question is consistently misread in such a way as not to alter the nature or difficulty of the question, please follow the candidate's work and allow follow through for $\mathbf{A}$ and $\mathbf{B}$ marks. Deduct 1 mark from any $\mathbf{A}$ or $\mathbf{B}$ marks earned and record this by using the MR annotation. M marks are not deducted for misreads.
11. Unless the question asks for an answer to a specific degree of accuracy, always mark at the greatest number of significant figures even if this is rounded or truncated on the answer line. For example, an answer in the mark scheme is 15.75 , which is seen in the working. The candidate then rounds or truncates this to $15.8,15$ or 16 on the answer line. Allow full marks for the 15.75 .
12. Ranges of answers given in the mark scheme are always inclusive.
13. For methods not provided for in the mark scheme give as far as possible equivalent marks for equivalent work. If in doubt, consult your Team Leader.
14. Anything in the mark scheme which is in square brackets [...] is not required for the mark to be earned, but if present it must be correct.


| Question |  | Answer | Marks | Part Marks and Guidance |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | (c) | $-2.6,2.6$ ( $\pm 0.1$ ) | 2 | B1, B1 (or ft their curve) If 0 scored, M1 evidence of reading from $y=4$ |  |
| 4 | (a) | 28 | 2 | M1 for $0.8 \times 35$ or $£ 7$ |  |
| 4 | (b)* | Clear correct explanation with conclusion that it is not a $30 \%$ discount <br> e.g. $0.8 \times 0.9=0.72$. This is a $28 \%$ discount, not $30 \%$. | 3 | 2 for correct complete working 1 for either 30\% reduction wo (£25.20) | but no conclusion ked out (£24.50) or $20 \%$ then $10 \%$ |
|  | (c)* | Compares offers and offers clear explanation with conclusion that buy two get one free is better. <br> E.g. Buy two get one free is one third off (33.3..\%). Buy one and get one half price mean getting two and paying for one and a half - this is one quarter off (25\%). The first offer is better. | 3 | 2 for correct complete working 1 for getting one offer into a fo with the other (e.g. using fraction | but no conclusion rm in which it could be compared ons or percentages). |


| 5 | (a) |  | $1: 1.5 \text { or } 1: \frac{3}{2} \text { or } 1: 11 / 2$ | 2 | M1 for $12 \div 8$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | (b) | (i) | $\frac{2}{5}$ | 1 |  |  |
|  |  | (ii) | $\frac{14}{5} \text { o.e. }$ | 1 |  |  |
|  | (c) | (i) | 30, 15 | 1,1 |  |  |
|  |  | (ii) | $\frac{15}{64} \text { oe }$ | 2 | M1 for multiplying by a power of $1 / 2$ |  |
| 6 | (a) |  | [ $\mathrm{x}=\mathrm{]}-5.5$ oe | 3 | M2 for $2 x=-11$ oe OR <br> M1 for $2 x-10$ <br> M1 for getting numbers or $x$ on one side only M1 for correct FT from $\mathrm{kx}+\mathrm{c}=\mathrm{n}$ | to maximum 2 marks |


|  | (b) |  | 2, 4 | 4 | M2 for correct factors $(x-4)(x-2)$ <br> OR <br> M1 for factors which multiply to give two correct terms in $x^{2}-6 x+8$ B1, B1 | Can be solved by completing square or use of formula <br> M2 for $\frac{6 \pm \sqrt{4}}{2}$ <br> OR M1 for $\frac{6 \pm \sqrt{6^{2}-4 \times 1 \times 8}}{2 \times 1}$ condone 1 error <br> OR M2 for $(x-3)^{2}-1=0$ oe OR M1 for $(x-3)^{2}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | (c) |  | $4 x-4$ | 3 | M1 for evidence of splitting shape into rectangles or for 2x <br> AND <br> M1 for $x-2$ soi by 2(x-2) or $2 x-4$ or $2 x-2$ |  |
| 7 | (a) |  | 5.7[4....] | 3 | $\begin{aligned} & \text { M2 } \sqrt{ }\left(7^{2}-4^{2}\right) \\ & \text { OR } \\ & \text { M1 } 7^{2}-4^{2} \end{aligned}$ | SC1 for any Pythagoras statement |
|  | (b) |  | 34.8[4...] | 3 | M2 for $\sin ^{-1} \frac{4}{7}$ <br> OR M1 for $\sin C=\frac{4}{7}$ | Allow correct use of tan or cos with their (a) for method marks $\text { eg } \cos C=\frac{\text { their }(a)}{7}$ |
| 8 | (a) | (i) | Circle centre origin Radius 3 | $\begin{aligned} & \hline \text { M1 } \\ & \text { A1 } \end{aligned}$ |  | Judge by eye |
|  |  | (ii) | $x^{2}+y^{2}=9$ | 2 | M1 for $x^{2}+y^{2}$ |  |
|  | (b) |  | Horizontal translation <br> 1 to right (graph through ( $0,-1$ )) | $\begin{aligned} & 1 \\ & 1 \end{aligned}$ |  | Judge by eye |


| 9 |  | 6.6 or 6.64 | 3 | M1 for length sf is 1.879... (or reciprocal 0.532...) <br> AND M1 for vol sf is their length sf cubed | Alternative method <br> M1 for $\frac{4 \pi}{3} \times 6371^{3}$ or $\frac{4 \pi}{3} \times 3390^{3}$ <br> AND M1 for dividing their Earth volume by their Mars volume |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 10 |  | $n^{2}+2 n o e$ | 2 | ```M1 for n}\mp@subsup{n}{}{2}\mathrm{ or 2 (nd difference = [+]2 OR for factor n in expression for nth term``` |  |
| 11 |  | $\sqrt{11}$ | 4 | M1 for $1^{2}+3^{2}$ AND M1 for their $B D^{2}+1^{2}$ AND M1 for 11 (can be implied by3.32...) |  |
| 12 | (a) | At intersection points, both equations are true So solution of simultaneous equations gives intersection points | $\begin{aligned} & \hline \text { M1 } \\ & \text { A1 } \end{aligned}$ |  |  |
|  | (b) | $(0,0)$ and ( 100,10000 ) | 5 | M1 for eliminating $y$ AND M1 for $x^{2}-100 x=0$ AND M1 for factorising A1, A1 for each pair of values |  |
|  | (c) | 2 | 1 |  |  |
| 13 |  | Complete proof | 5 | M1 for Length $(b-a)$ <br> M1 for Width $\left(\frac{1}{a}-\frac{1}{b}\right)$ <br> M1 for Area $(b-a)\left(\frac{1}{a}-\frac{1}{b}\right)$ <br> M1 for $\frac{a}{b}+\frac{b}{a}-2$ oe | $\frac{1}{a}$ and $\frac{1}{b}$ even if not subtracted <br> eg $(b-a) \frac{(b-a)}{a b}$ |


| 14 | (a) | Correct explanation | 1 |  | eg GC is the radius and this is 4 cm |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | (b) | 17.2[168..] | 8 | M1 for $\cos G C D=\frac{1}{4}$ <br> A1 for $\angle \mathrm{GCD}=75.5^{\circ}($ need not be rounded) <br> AND <br> M1 for area triangle GCD = $\frac{1}{2} \times 2 \times 4 \times \sin 75.5$ <br> A1 for $3.87 . . \mathrm{cm}^{2}$ <br> AND <br> M1 for area sector GCE = $\frac{75.5}{360} \times \pi \times 4^{2}$ <br> A1 for 10.54... <br> AND <br> M1 for $2 \times$ their 10.54.. their 3.87.. |  |

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