

Mark Scheme (Results)

Summer 2014

Pearson Edexcel International GCSE in Mathematics B Paper 1 (4MB0/01)

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Summer 2014
Publications Code UG039435
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# **General Marking Guidance**

- All candidates must receive the same treatment. Examiners must mark the first candidate in exactly the same way as they mark the last.
- Mark schemes should be applied positively. Candidates must be rewarded for what they have shown they can do rather than penalised for omissions.
- Examiners should mark according to the mark scheme not according to their perception of where the grade boundaries may lie.
- There is no ceiling on achievement. All marks on the mark scheme should be used appropriately.
- All the marks on the mark scheme are designed to be awarded. Examiners should always award full marks if deserved, i.e. if the answer matches the mark scheme.
   Examiners should also be prepared to award zero marks if the candidate's response is not worthy of credit according to the mark scheme.
- Where some judgement is required, mark schemes will provide the principles by which marks will be awarded and exemplification may be limited.
- Crossed out work should be marked UNLESS the candidate has replaced it with an alternative response.

### Types of mark

- o M marks: method marks
- o A marks: accuracy marks
- B marks: unconditional accuracy marks (independent of M marks)

#### Abbreviations

- o cao correct answer only
- o ft follow through
- o isw ignore subsequent working
- o SC special case
- o oe or equivalent (and appropriate)
- o dep dependent
- o indep independent
- o eeoo each error or omission

#### No working

If no working is shown then correct answers normally score full marks

If no working is shown then incorrect (even though nearly correct) answers score no marks.

# With working

If there is a wrong answer indicated on the answer line always check the working in the body of the script (and on any diagrams), and award any marks appropriate from the mark scheme.

If it is clear from the working that the "correct" answer has been obtained from incorrect working, award 0 marks.

Any case of suspected misread loses A (and B) marks on that part, but can gain the M marks.

If working is crossed out and still legible, then it should be given any appropriate marks, as long as it has not been replaced by alternative work.

If there is a choice of methods shown, then no marks should be awarded, unless the answer on the answer line makes clear the method that has been used.

If there is no answer on the answer line then check the working for an obvious answer.

# Ignoring subsequent work

It is appropriate to ignore subsequent work when the additional work does not change the answer in a way that is inappropriate for the question: eg. Incorrect cancelling of a fraction that would otherwise be correct.

It is not appropriate to ignore subsequent work when the additional work essentially makes the answer incorrect eg algebra.

Transcription errors occur when candidates present a correct answer in working, and write it incorrectly on the answer line; mark the correct answer.

# Parts of questions

Unless allowed by the mark scheme, the marks allocated to one part of the question CANNOT be awarded in another.

<b>Question Number</b>	Answer	Notes	Marks
1	$\frac{4(x+3)}{x(x+3)}$	M1	
	<b>Note:</b> Award M1 for the correct factorisation of <b>either</b> the numerator or denominator		
	$\frac{4}{x}$	A1 2	2
2	$117\pi = \pi r^2 \times 13 \tag{o.e}$	M1	
	<b>Note:</b> Allow a numerical value of $\pi$ (3.14 or better)		
	$r = 3 \mathrm{cm} \mathrm{(cao)}$	A1 2	2
3	$\frac{625}{1000}$ OR 0.625	M1	
	Note: Accept any equivalent correct fraction.		
	$\frac{5}{8}$	A1 2	2
	<b>Note:</b> No isw if the candidate goes on after the correct answer		
4	$\frac{360}{24}$ or $180 - \frac{180 \times (24 - 2)}{24}$	M1	
	<b>Note:</b> $180 - \frac{360}{24}$ earns M0 unless recovered		
	15°	A1 2	2
-	2n n 1 2 (nomeno denom)	N/1	
5	2x = x + 3 (remove denom.)	M1	

	Note: $6 = x + 3$ earns M1 $(x =) 3$	A1	2	2
	Notes: 1. Answer only seen – full marks 2. Correct answer seen but working wrong, award M0,A0			
6(a)	$0.0177$ or $1.77 \times 10^{-2}$	B1	1	
<b>6(b)</b>	0.018	B1	1	2
7	N A 180+48			
	$180^{\circ} + 48^{\circ}$ or $360^{\circ} - (180^{\circ} - 48^{\circ})$ OR diagram indicating reflex angle $\angle NAB$			
	<b>Note:</b> Where a diagram is drawn, we need to clearly see a numerical value assigned to the reflex angle $\angle NAB$ (It does not need to be simplified)	M1		
	228° OR S48W	A1	2	2
8	$a^4$ as numerator or 4 as denominator	M1		

	<b>Note:</b> 1. Ignore any coefficient before $a^4$ for this M mark. $6 \times \frac{2}{6}$		
	2. $a^{6\times\frac{2}{3}}$ does not earn the M mark (yet) $\frac{a^4}{4}$	A1 2	2
	<b>Notes:</b> 1. Do not isw.  2. $\frac{a^4}{2^2}$ earns M1, A0 (unless continues to required solution)		
9	$\begin{bmatrix} 2(n+1)-1 \end{bmatrix} - \begin{bmatrix} 2n-1 \end{bmatrix} \qquad \text{(o.e)}$ <b>OR</b> Any two correct consecutive numerical terms <b>Notes:</b> 1. (o.e.) $(2n+1)-(2n-1)$ 2. Award M1 for $2n-1=a+(n-1)d$ and comparing coefficients	M1	
	difference = $\pm 2$	A1 2	2
10	Two of $30 = 5 \times 6$ , $36 = 6 \times 6$ , $138 = 23 \times 6$ OR  Two of prime factors, factor trees, compound division or list of factors	B1	
	Note: Award full marks for a correct answer only seen	B1	2
11	$x^2 + bx - ax - ab = 3bx   (expand)$	M1	
	$x^2 + bx - 3bx = ax + ab $ (isol. terms in a)	M1 (DEP)	

On		
OR		
$x - a = \frac{3bx}{x + b}$	M1	
$x-a=\frac{1}{a+b}$		
	251 (222)	
$\int a - x = 3bx$ or $a = 3bx$	M1 (DEP)	
$a = x - \frac{3bx}{x+b}$ or $-a = \frac{3bx}{x+b} - x$		
OR		
3bx + a(x+b) = x(x+b)	M1	
a(x+b) = x(x+b) - 3bx	M1 (DEP)	
$a = \frac{x^2 - 2bx}{x + b}  \text{(o.e.)}$	A1 3	3
<b>Note:</b> 1. An example of (o.e.) $a = -\frac{x(2b-x)}{x+b}$		
2. $3bx-bx$ must be simplified before the final A mark can be awarded		
3. Do <b>not</b> isw		

12	$\angle CDA = 70^{\circ}$ (Cyclic quad.)	B1		
	$\therefore \angle COD = 40^{\circ} \text{ (Isos. Triangle)}$	B1		
	<b>Note:</b> For 'isosceles triangle' $CO = OD$ and triangle sufficient for reason			
	OR .	D1		
	$\angle CBD = 20^{\circ} \ (\angle \text{ in semi-circle for } \angle ABD)$	B1		
	$\therefore \angle COD = 40^{\circ} \text{ (angle at centre)}$	B1		
	Both of above reasons	B1	3	3
	<ol> <li>Notes: 1. Accept the required angle (COD) marked on the diagram for answer</li> <li>2. Reasoning(s) must be consistent with a correctly calculated angle</li> <li>3. Unless the candidate starts again, an incorrectly calculated angle (because of wrong reasoning) condemns further work.</li> <li>4. Opp angle of a quadrilateral is not a sufficient reason.</li> <li>5. Do not accept 'angle sum of a triangle' as a reason unless it is used with CO = OD</li> <li>6. Accept a single letter notation (D) for ∠CDA</li> </ol>			
	SC: One reason and correct answer, B1 B1 B0 No reasons and correct answer B1 B0 B0			
13	One of $\sqrt{245}$ or $\sqrt{45}$ rewritten as $\sqrt{5 \times 7 \times 7}$ or $\sqrt{5 \times 3 \times 3}$			
	(oe, eg $7\sqrt{5}$ or $3\sqrt{5}$ )	M1		
	$7\sqrt{5}-3\sqrt{5}$	M1		
	<b>Note:</b> Condone $7\sqrt{5} - 3\sqrt{5} = 7 - 3\sqrt{5}$			_
	$4\sqrt{5}$	A1	3	3
	Note: The A mark is dependent on the <b>first</b> M mark.			
14	$0.59 \times \pi \times 110 \text{ m/min}$ OR $59 \times \pi \times 110 \text{ cm/min}$			

	(ie distance travelled in 1 min)	M1	
	"0.59× $\pi$ ×110"× $\frac{60}{1000}$ OR "59× $\pi$ ×110"× $\frac{60}{100000}$ ie $\begin{cases} conv \text{ to km} \\ conv \text{ to hrs} \end{cases}$	M1 (DEP)	
	12.2 km (awrt)  SC: 3.89(or better) award M0, M1, A0	A1 3	3
15	$280 = \left(\frac{h}{9}\right)^{2} \times 70 \text{ (o.e.)} \qquad \sqrt{\left(\frac{280}{70}\right)} \text{ or } \sqrt{4} \text{ or } \frac{9.44}{4.72} \text{ seen}$	M1	
	$\therefore h = 9\sqrt{\frac{280}{70}}$	M1 (DEP)	
	<ul> <li>h = 18 cm (awrt)</li> <li>Note: If volumes are compared and the incorrect formula for the volume of a cone is used, a maximum of the first M mark can be awarded.</li> </ul>	A1 3	3

16	$9 = k \times 2^3 \qquad \text{(o.e)}$		M1		
	$k = \frac{9}{8}$ , 1.125	$9x^3 = 8 \times 72  \text{(or better)}$	A1		
	<b>Notes:</b> 1. $k = 1.13$ (or better) for A mark 2. If $9 \times k = 2^3$ , award M1 $k = \frac{8}{9}$ or 0.88 award A1				
	9		M1 (DEI	D)	
	$x = \sqrt[3]{\frac{72}{"\left(\frac{9}{8}\right)"}}$ (o.e: (taking cube root))	$x = \sqrt[3]{\frac{8 \times 72}{9}}$	WII (DEI		
	x = 4		A1	4	4
17	Balancing either $x$ or $y$ in the two equations	isolating x or y e.g. $x = 15-3y$ or $y = 2x-2$	M1		
	Correctly deciding whether to add or subtract	subst expression for x or y to obtain an equation in one unknown	M1 (DEI	?)	
	<b>Note:</b> Allow a total of 1 slip in both M marks.		_		
	2		A 1		
	$   \begin{array}{r}     x = 3 \\     y = 4   \end{array} $		A1 A1	4	4
	Note: All answers only seen for full marks. One no marks	only correct answer with no working seen earns	711	T	
18(a)	40		B1		

	6			A1 ft 3	4
	"15" – 9	9+"3"+ <i>x</i> = 18	$45 + 5 \times "3" + 5x = 54 + 6x$	M1 (DEP)	
19(b)	5×"3" (o.e.)	$\frac{1}{6}(9 + "3" + x) = 3$	$\frac{5}{6}(9+"3"+x)=9+x$	M1	
19(a)	3			B1 1	
	Note: Allow a tolerance	te of $\frac{1}{2}$ small square on the graph for	or B marks in part (b)		
	7			B1 2	4
18(b)	0.5			B1	
	60			B1 2	

missing)		
$\sqrt{41}$ OR 6.40 (or better)  Note: This is an independent B mark and can be earned from previous incorrect working	B1	
<ul> <li>1.18, -0.425</li> <li>Note: 1. Accept answers which round to the required answers (no penalty for failing to correct)     2. Overcorrecting will always be penalised     3. Unrounded correct answers seen in the body of the script, then over-corrected, award corresponding A marks.</li> <li>SC: The candidate may try and factorise the given quadratic. The M mark only is available as follows: You need to multiply out their incorrect bracketed terms. If the resultant quadratic gives two of their three terms of "4x²-3x-2" then award the M mark.</li> </ul>	A1, A1 4	4

21(a)	$\begin{array}{ c c c c c c c c c c c c c c c c c c c$		
	Notes: 1. 38-x can be anywhere inside the crescent to the left 2. 27-x can be anywhere inside the crescent to the right 3. The numerical value 5 can be anywhere outside the two circles 4. Ignore any other values or expressions in x that you see	B1 1	
21(b)	" $(38-x)$ "+ $x$ + " $(27-x)$ "+ $5 = 50$ (38 + 27 + 5) - 50 Note: $38 + 27 + x + 5 = 50$ can earn method here	M1	
	x = 20	A1 2	
21(c)	Prob = $\frac{38 - "20"}{50}$ Notes: 1. "20" must be a positive value for method to be earned 2. If this fraction is combined with another fraction then method is lost	M1	
	$\frac{18}{50}$ (o.e.), 0.36, 36%	A1 ft 2	5

22(a)	$\overrightarrow{AB} = \begin{pmatrix} 1 \\ 2 \end{pmatrix}$	B1	1	
	Note: Penalise $\left(\frac{1}{2}\right)$			
22(b)	$\overrightarrow{OC} = 2" \begin{pmatrix} 1 \\ 2 \end{pmatrix} " + \begin{pmatrix} 1 \\ 1 \end{pmatrix} \begin{pmatrix} = \begin{pmatrix} 3 \\ 5 \end{pmatrix} \end{pmatrix}$	M1		
	(3, 5)	A1	2	
22(c)	$\left(\overrightarrow{AC} = 2 \times "\overrightarrow{AB}" = \begin{pmatrix} 2\\4 \end{pmatrix}\right)$			
	$\sqrt{"2"^2 + "4"^2}$ $\sqrt{"3"^2 + "5"^2}$	M1		
	$\left  \overrightarrow{AC} \right  = 4.47 \text{ (awrt)}$	A1	2	5
23(a)	Penalise ncc ONCE only in the question			
25(a)	$\cos 15 = \frac{11}{AB} \text{ (o.e.)}$	M1		
	<b>Note:</b> Equivalent methods may involve sin 15, sine rule, tangent + Pythagoras The M mark awarded for any correct trig/Pythagorean statement which involves the side AB. (It does no to be evaluated).			
	11.39 -> <b>11.4 cm</b>	A1	2	

23(b)	AC = 11  x tan  15  (oe)  (=2.947)	$AC = \sqrt{11.39^{2} - 11^{2}} = 2.955$	$\angle DCB + \angle BDC = 165^{\circ}$	M1		
	<i>DB</i> = "11.39"-"2.947"	<i>DB</i> = "11.39"-"2.995"	$DB = \frac{11 \times \sin" 37.5"}{\sin" 127.5"}$	M1 (D	DEP)	
	Accept any of the following answ	vers: 8.41, 8.44 or 8.45		A1	3	5
24(a)	Construction arcs			M1		
	<b>Note:</b> the required number of con	mpass construction arcs are require	ed			
	Perpendicular bisector drawn into	ersecting BC and also AC		A1	2	
	Notes: 1. For the A mark, there the triangle. 2. Must be a continuous	should be no daylight between the	e line and the overlay within			
24(b)	Construction arcs	(100 00000) 1110 101 1110		M1		
	<b>Note:</b> the required number of con	mpass construction arcs are require	ed			
	Angle bisector drawn (from B and	l intersecting AC)		A1	2	
	the triangle.	should be no daylight between the	•			
	2. An incorrect line draw closely at construction 3. Must be a continuous	,	M1 has not been earned (look			
24(c)	Region <b>R</b> within $\triangle ABC$ shaded <b>a</b>	,		B1 ft	1	5
		vithin the triangle, all the region to th their (complete) angle bisector.	the left of the perpendicular			

25(a)	$\frac{£1}{2.5}$		M1		
	£0.40		A1	2	
	<b>Note:</b> Accept £0.4 but do not accept 40p				
25(b)	One of 1.2×2.5kg or 1.11×£1  One of "0.40"×1.11 or "0.40"÷1.2				
		Note: "0.40" < £1.00			
	$\frac{\pounds 1.11}{3}$	"0.40"×1.11 1.2	M1 (E	DEP)	
	£0.37		A1	3	5
26(a)	$2 \times (-3)^3 + 13 \times (-3)^2 + 27 \times (-3) + 18$	$(-3)^3 + 13 \times (-3)^2 + 27 \times (-3) + 18$ Dividing the cubic by $(x+3)$ and arriving at a quotient of $2x^2 + 7x$			
		Note: Allow synthetic division method  -3			
	= 0	A quotient of $2x^2 + 7x + 6$	A1	2	
	<b>Note:</b> If we see four numerical values they must be $-54+117-81+18$ . If any part of this Expression is incorrect then A0 Stating = 0 without numerical values earns the A mark	<b>Note:</b> Using the synthetic division method, the entries in the fourth row must be 2 7 6			

26(b)	$2x^2 + 7x$	3	0 2	13 -6	27 -21	18 -18	M1		
	$2x^2 + 7x + 6$			,			A1		
	<b>Note:</b> These two marks can be earned again here if shown in part (a)								
	Factorising a trinomial quadratic				M1 (II	NDEP)			
	<b>Note:</b> If the candidates two bracketed terms are not the required terms they can still earn the M mark here. You need to multiply out their incorrect bracketed terms. If the resultant quadratic gives two of their three terms of $"2x^2 + 7x + 6"$ then award the M mark.								
	(x+3)(2x+3)(x+2)				A1	4	6		
	<b>Notes:</b> 1. Allow the A mark for $(x+3)(2x+3)(x+2) = 0$ but, if the candidate goes on to solve their correct equation, they lose the last A mark.  2. For this mark, we will allow a missing trailing bracket e.g. $(x+3)(2x+3)(x+2)$								

27(a)		(3/5) Hit	
	3 Hit	$\left(\frac{2}{5}\right)$ Miss	
	4		
	$\left(\frac{1}{4}\right)$ Miss	$\frac{\binom{3}{5}}{}$ Hit	
		Miss	
		$\left(\frac{2}{5}\right)$	
	1st Shot	2nd Shot	B2(-1eeoo) 2
	<b>Note:</b> -1 penalty for each For ePen: One pen	incorrect pair. (Not for an individual probability) alty implies B1, B0 NOT B0, B1	

27(b)	$\frac{3}{4}$ × " $\frac{2}{5}$ " (o.e.)		M1		
	<b>Note:</b> This probability pair must not be embedde				
	$\frac{6}{20}, \frac{3}{10}, 0.3, 30\%$ $\frac{3}{4} \times \frac{2}{5} + \frac{1}{4} \times \frac{3}{5} + \frac{3}{4} \times \frac{3}{5}$	A1	2		
27(c)	$\frac{3}{4} \times \frac{2}{5} + \frac{1}{4} \times \frac{3}{5} + \frac{3}{4} \times \frac{3}{5}$				
	two "correct" products added from their diagram	$\frac{1}{4}$ "×" $\frac{2}{5}$ "	M1		
	all three "correct" products added from their diagram		M1 (I	DEP)	
	$\frac{18}{20}$ , $\frac{9}{10}$ , 0.9, 90%		A1	3	7
28(a)	$y = x^2 + (10 - x)(20 - x)$	$y = 20 \times 10 - x(10 - x) - x(20 - x)$	M1		
	$y = 2x^2 - 30x + 200    (c.c)$	<u>I</u>	A1	2	
	<b>Notes:</b> 1. Algebraic errors in the candidate's working loses this A mark 2. If " $y =$ " does not appear in the candidate's working then A mark is lost				
28(b)	$\frac{dy}{dx} = 4x - 30$ (1 term correctly differentiated from their y)				
	4x-30   = 0	M1 (I	DEP)		
	<b>Note:</b> Must be a linear equation in <i>x</i> for method.				
	x = 7.5	A1	3		
28(c)	$2 \times "7.5"^2 - 30 \times 7.5 + 200$ (subst.)	$(10-"7.5")\times(20-"7.5")+"7.5"\times"7.5"$	M1		
	87.5 cm <sup>2</sup>		A1	2	7
		TOTAL 100 MARK	S		

